

# Beam-based optimization of accelerators

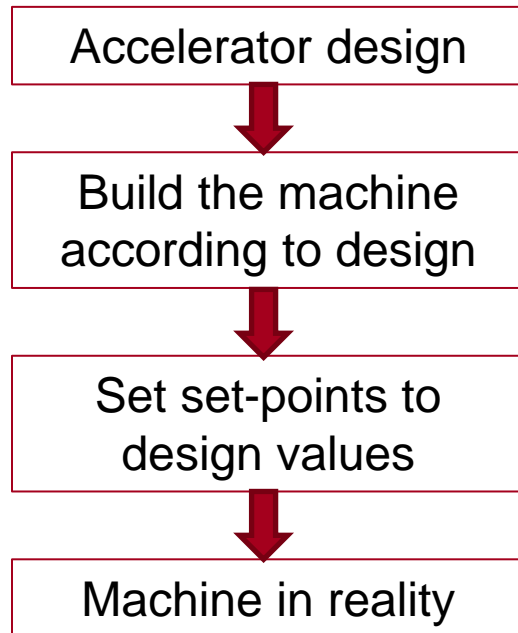
USPAS, Jan. 21-25, 2019

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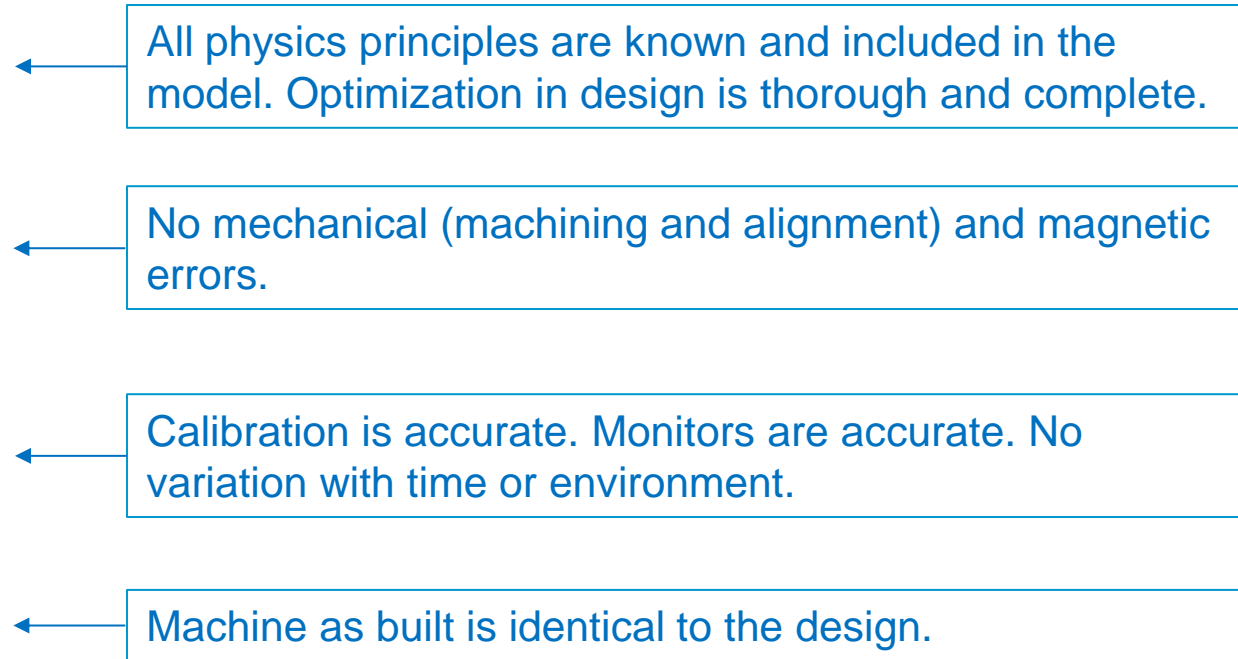
- Motivation
  - Beam based correction vs. beam based optimization
  - Manual tuning vs. automated tuning
- Online optimization algorithms
  - Iterative 1-dim scans
  - Nelder-Mead simplex
  - Robust Simplex
  - Robust conjugate direction search (RCDS)
  - Extremum seeking
  - Genetic algorithm and particle swarm optimization
  - Bayesian optimization
- Applications

# Achieving optimal accelerator performance

The process:



The ideal scenario:



However, the reality is never ideal.

Solutions: (1) Beam-based correction.  
(2) Beam-based optimization (tuning).

# Beam based correction

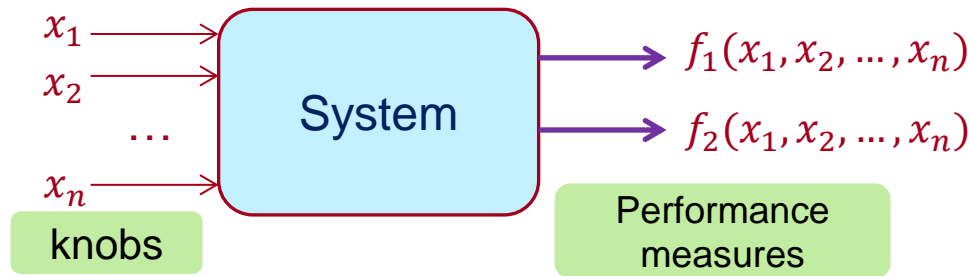
**Beam based correction:** correct the operating condition of a subsystem toward the ideal (design) condition through beam based measurements and a deterministic procedure.

	Actuators (knobs)	Diagnostics (monitors)	Deterministic method	Target
Orbit correction	Orbit correctors	BPMs	Orbit response matrix	Ideal orbit
Optics correction	Quadrupole correctors	Beta, phase advance, orbit response matrix	Response (Jacobian) matrix	Design optics

What if any of diagnostics, deterministic method, or ideal target is missing?

# Beam based optimization – tuning

**Beam based optimization (tuning):** adjust the operating condition to optimize machine performance directly.



The system is a black-box. The performance measures are evaluated by dialing in the knob setpoints and observing performance with diagnostics.

Machine tuning is a multi-variable and (potentially) multi-objective optimization process. The function(s) is evaluated through the machine.

# Manual tuning vs. automated tuning

## Manual tuning

Knob changing by human hands, data processing and decision making by human brain.

## Automated tuning

Knob changing, data processing, and decision making all by computer.

### Manual tuning

Slow

Human dependent

Limited to small problems  
(few knobs)

### Automated tuning

Fast

Human independent

Scalable to large problems

# Challenges to automated tuning algorithms

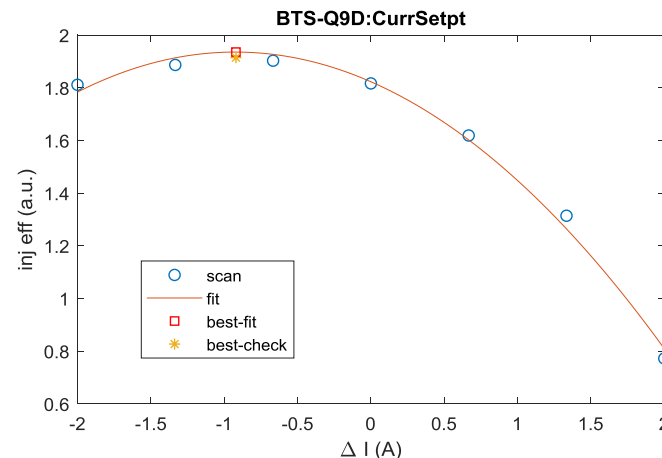
- Noise – functions evaluated on machine have noise.
  - Most of the traditional methods are designed for smooth functions.
- Efficiency
  - Need to converge to the optimum fast.
- Safety, reliability, robustness
  - Survive occasional outliers.
  - Cause no disaster when machine mal-functions.

An early work on automated tuning:

L. Emery et al, PAC2003, implemented 1D scan and the downhill simplex method.

# Iterative 1D scans

- Scan one variable at a time
  - Specify parameter range
  - Specify step size or number of points
  - Range and step size vary with parameter and depend on the problem
    - Could be inefficient with unnecessarily large range or fine step size
    - Could fail to locate the optimum if parameter range is too narrow or step size too large
- Iterative parameter scan may be very inefficient as the change of one parameter can void the scan results of other parameters.

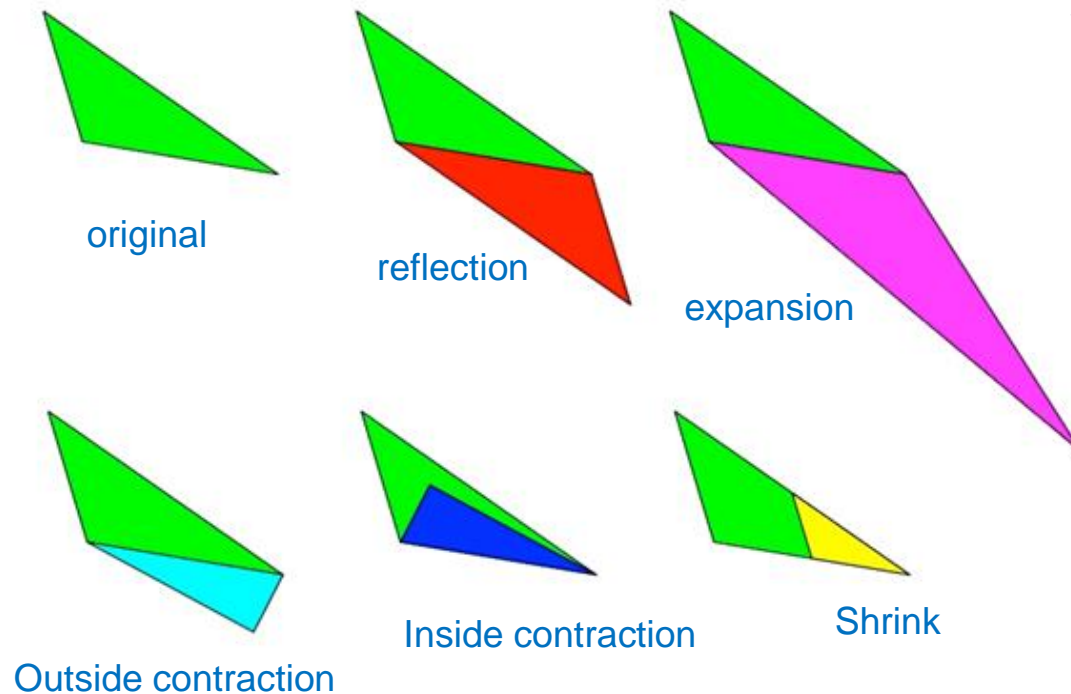




# Nelder-Mead Simplex method

- The NM Simplex method is typically very effective for smooth functions.
- But since it relies on function value comparisons, its convergence course can be changed by noise.

Worst vertex



With noise:

- the determination of the worst-value vertex may be incorrect
- the decision on the type of operation may also be incorrect.
- May lead to frequent shrink operation and further suffer from noise

J. A. Nelder and R. Mead, The Computer Journal 7, 308 (1965).

# Robust Simplex – improving robustness against noise

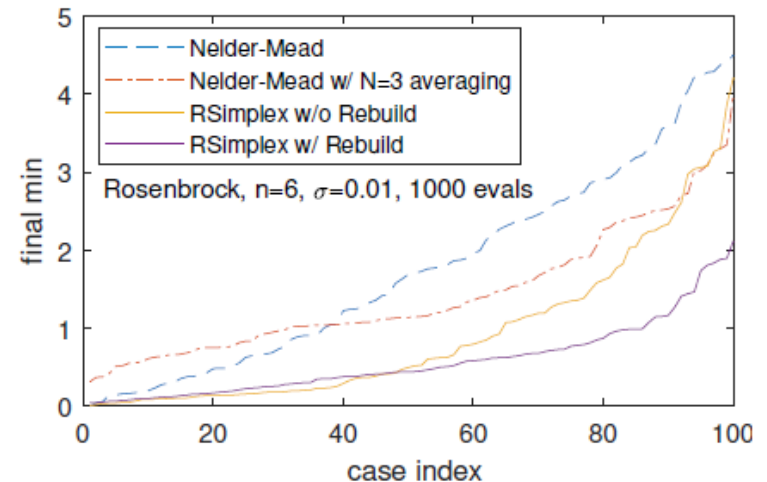
- Effect of noise to the Nelder-Mead simplex method can be mitigated.
  - Improve data accuracy when necessary with averaging

The difference between the sample averages of two random variables,  $\bar{X}_1 - \bar{X}_2$ , satisfies

$$\mathcal{N}(\mu_1 - \mu_2, \Sigma^2), \quad \text{with } \Sigma^2 = \frac{\sigma_1^2}{N_1} + \frac{\sigma_2^2}{N_2}$$

The sign of  $\bar{X}_1 - \bar{X}_2$  is a good estimate of the sign of  $\mu_1 - \mu_2$  if  $|\bar{X}_1 - \bar{X}_2|$  is substantially larger than  $\Sigma$ .

X. Huang PRAB 21, 104601 (2018)



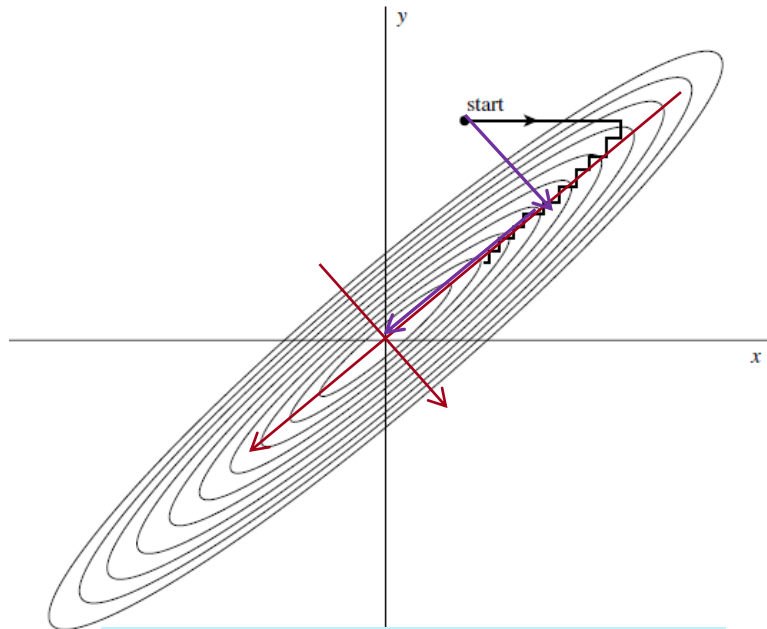
- Use multiple worst vertices when a winner cannot be easily determined (accept one that leads to successful reduction of the minimum)
- Use fitting of multiple points along a line to determine contraction operation if necessary
- Re-build the simplex when it shrinks to a certain limit

# The RCDS algorithm

- Robust conjugate direction search (RCDS)\* performs iterative search over conjugate directions with a robust (against noise), efficient line (1D) optimizer.
  - The conjugate direction set may be updated with Powell's method.
  - The 1D robust optimizer is designed to deal with noise.

\*X. Huang, J. Corbett, J. Safranek, J. Wu, "An algorithm for online optimization of accelerators", Nucl. Instr. Methods, A 726 (2013) 77-83.

# Search over conjugate directions



Inefficient search directions

It takes many tiny steps to get to the minimum when searching along  $x$  and  $y$  directions.

Efficient search directions: conjugate directions

A search over conjugate direction does not invalidate previous searches.

Directions  $\mathbf{u}$  and  $\mathbf{v}$  are conjugate if

$$\mathbf{u}^T \cdot \mathbf{H} \cdot \mathbf{v} = 0$$

with  $\mathbf{H}$  being the Hessian matrix of function  $f(\mathbf{x})$ ,

$$H_{ij} = \frac{\partial^2 f}{\partial x_i \partial x_j}.$$

Around the minimum

$$f(\mathbf{x}_m + \Delta\mathbf{x}) = f(\mathbf{x}_m) + \frac{1}{2} \Delta\mathbf{x}^T \cdot \mathbf{H} \cdot \Delta\mathbf{x}.$$

Powell's method can update the directions using past search results to develop a conjugate set.

\*W.H. Press, et al, Numerical Recipes

\*M.J.D. Powell, Computer Journal 7 (2) 1965 155

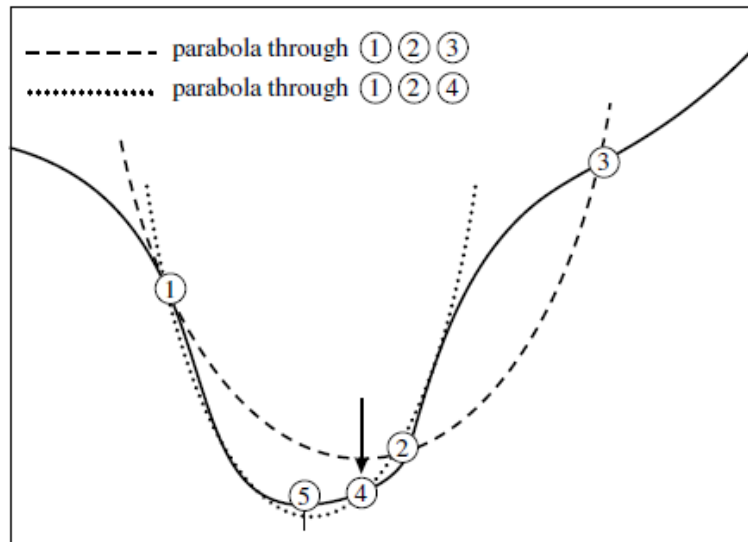
X. Huang, Jan. 21-25, USPAS, Knoxville, TN

# Anatomy of a line optimizer that is sensitive to noise

## Line optimizer – Brent's method

Step 1: Initially bracketing the minimum.

Step 2: Successive interpolation to converge to the minimum.



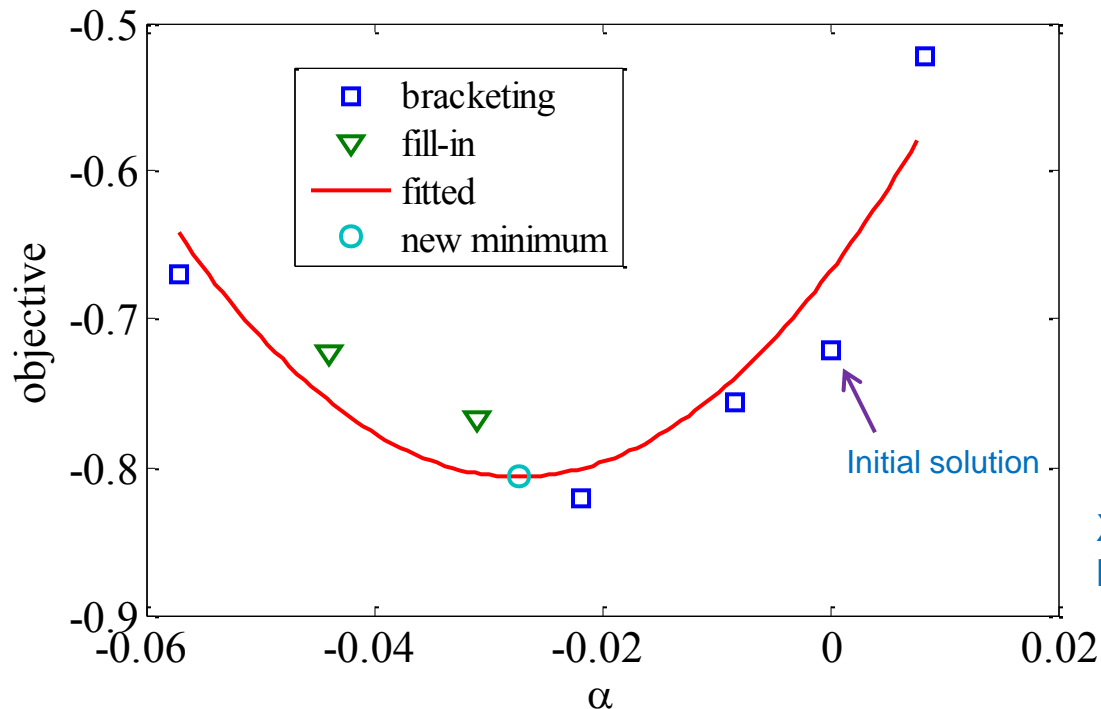
Inverse quadratic interpolation (figure from Numeric Recipes\*.)

With noise, the comparison of values in both steps can go wrong and the algorithm won't converge.

\*W.H. Press, et al, Numerical Recipes

# The robust 1D optimizer

The robust optimizer is aware of noise in bracketing and uses noise level to filter out outliers. Noise level is detected before optimization.



X. Huang et al, Nucl. Instr. Methods, A 726 (2013) 77-83.

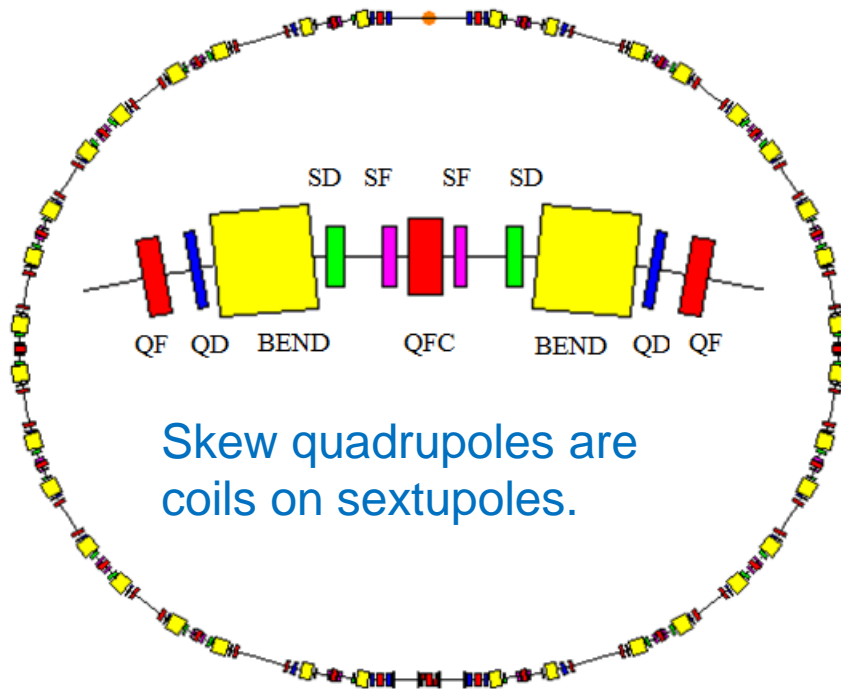
**Bracketing:** step size is increased in the search. Bracket ends are higher than minimum by 3 noise sigma.

**Fitting:** fill in additional points when necessary to better sample within the bracket and then fit a parabola.

- Parameters are bounded and normalized to  $[0, 1]$ 
  - Parameters in online optimization always have limited ranges.
  - Keeping parameters within pre-defined ranges is a safety measure.
  - Normalizing parameters makes algorithm code independent of actual problems
- Powell's method of automatic updating of conjugate direction set is implemented.
  - In real life problems usually only a few directions are replaced before terminating. So we hardly benefit from this procedure for online problems.
- The interface between the algorithm and a particular application is the objective function and a simple setup script.

# Testing the algorithm with a simulation problem

Testing problem: coupling correction for the SPEAR3 storage ring with skew quadrupoles.



Skew quadrupoles are coils on sextupoles.

The SPEAR3 storage ring

**Objective:** maximize beam loss over 6 seconds (Touschek loss rate  $\propto 1/\sigma_y$ ).

**Knobs:** 13 skew quads

**Setup:** (1) errors are added to 42 skew quadrupoles. Initially all 13 correcting skew quads are off, with coupling ratio of 0.9%.

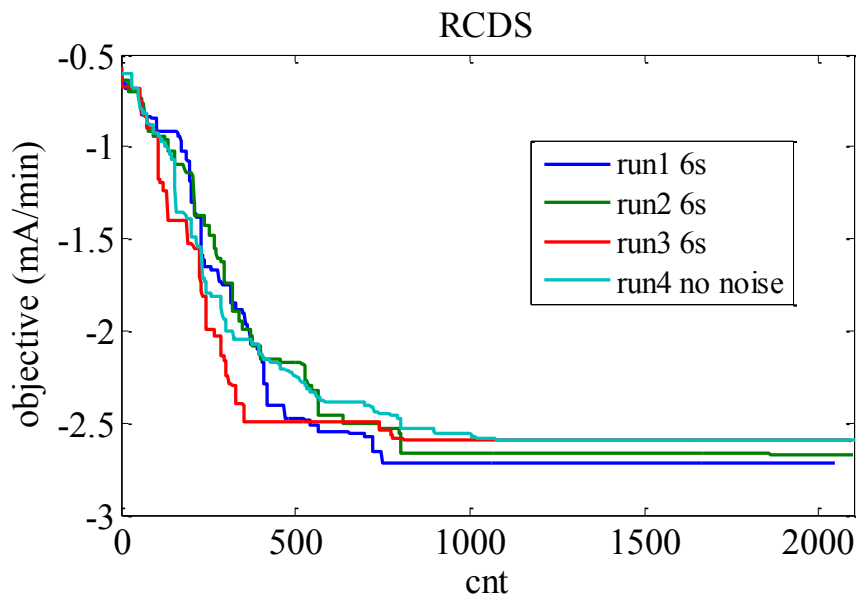
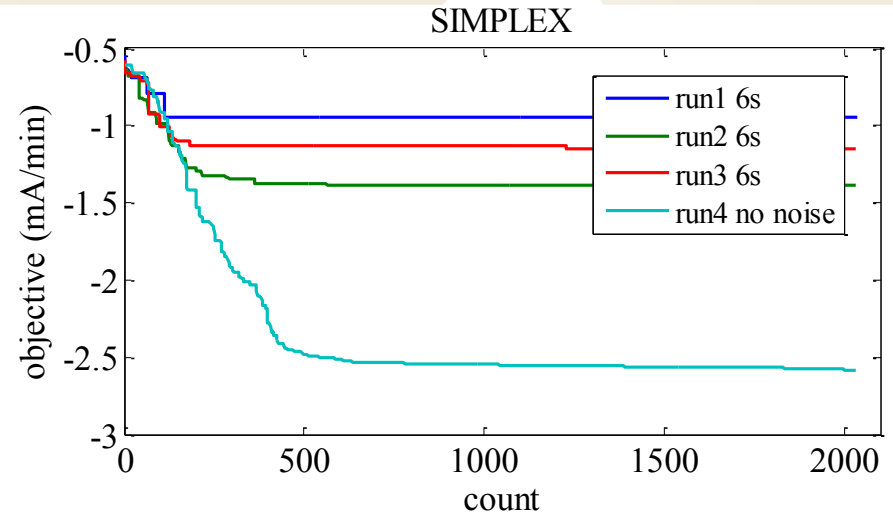
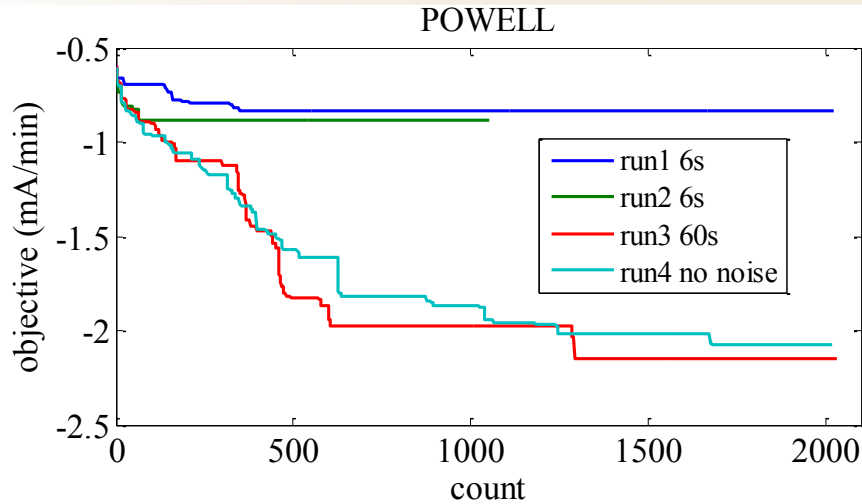
(2) Noise level for loss rate is about 0.06 mA/min, with initial loss rate at 0.6 mA/min.

(3) Initial conjugate direction set is from SVD of the Jacobian matrix of the orbit response matrix w.r.t. skew quads.

$J = USV^T$  Each column in **J** is for a skew quad. Conjugate directions are represented by columns in **V**.



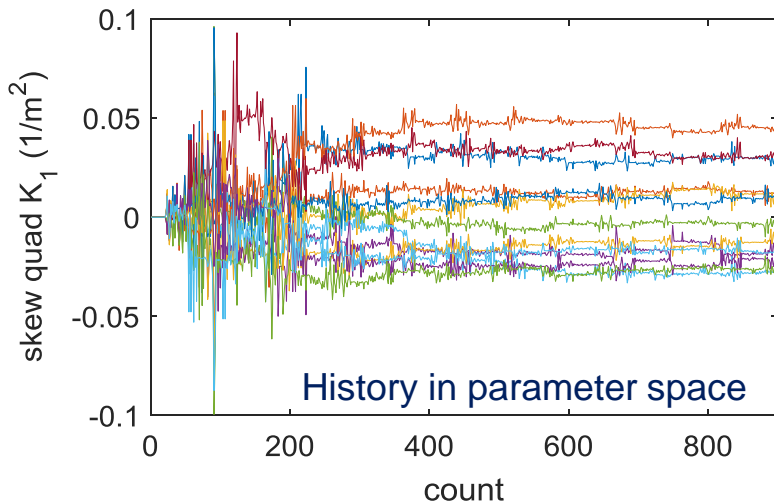
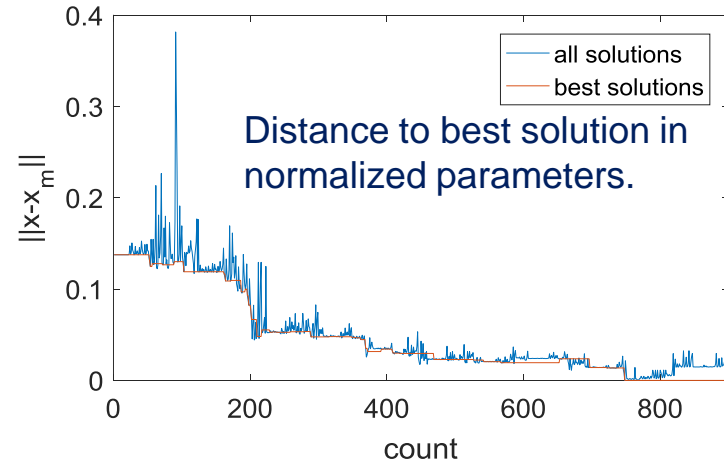
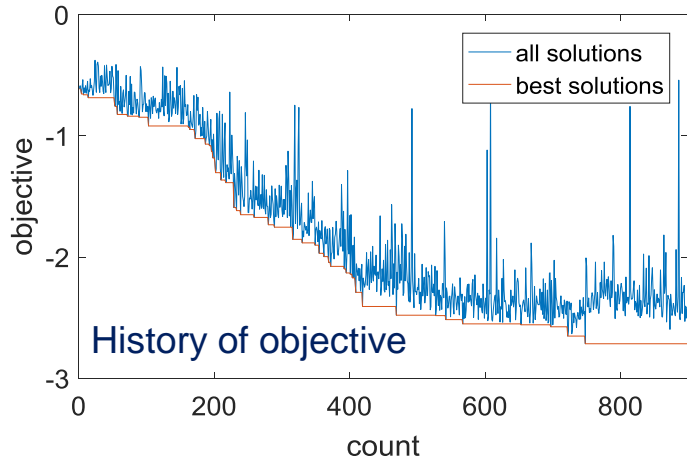
# Simulation results for three direct search methods



- (1) Showing history of the best solution.
- (2) The simplex method is efficient without noise, but fails to reach the minimum with noise.
- (3) Powell's method works without noise, but fails with noise. The initial direction set are individual skew quads.
- (4) The RCDS method is efficient with or without noise.**

The performances of algorithms for noisy problems depends on the problems.

# Detailed look of an RCDS run

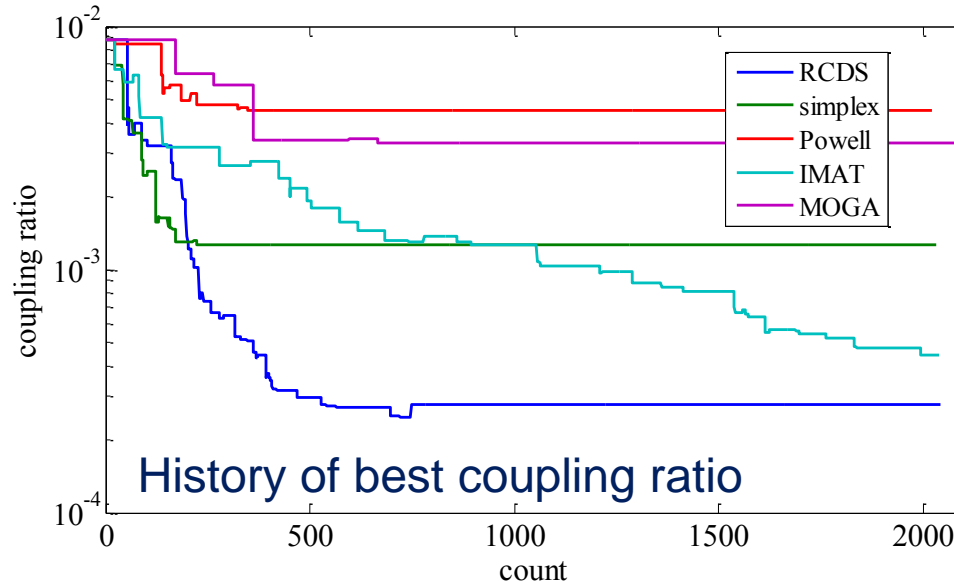


The algorithm converges fast but it does not stay right at the minimum – it keeps probing around.

So usually we need to sort the solutions and apply the best one to the machine.

# Comparison of algorithm performances

## Best performance for several algorithms

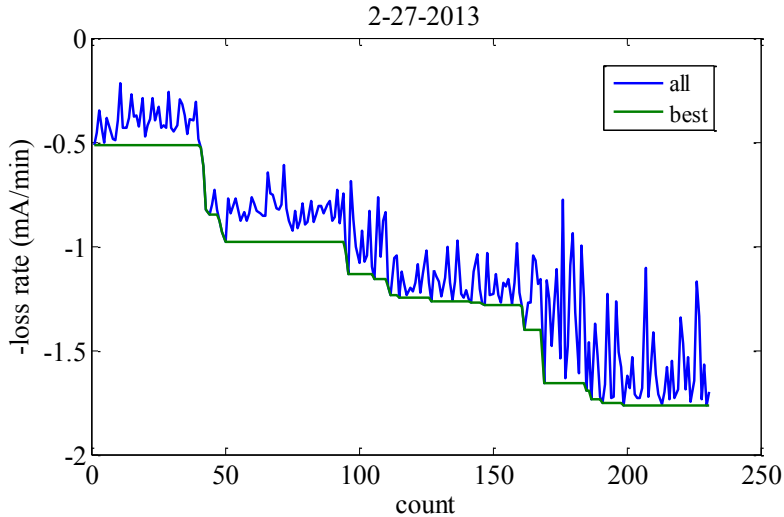


“IMAT”: iterative scan of each skew quad with the robust 1D optimizer. The difference between “IMAT” and “RCDS” clearly shows the power of using conjugate direction set for problems with highly coupled parameters.

Only “IMAT” and “RCDS” have steady gains toward the minimum - a manifest of the noise-resistance feature of the robust 1D optimizer.

# Coupling correction experiments on SPEAR3 with RCDS

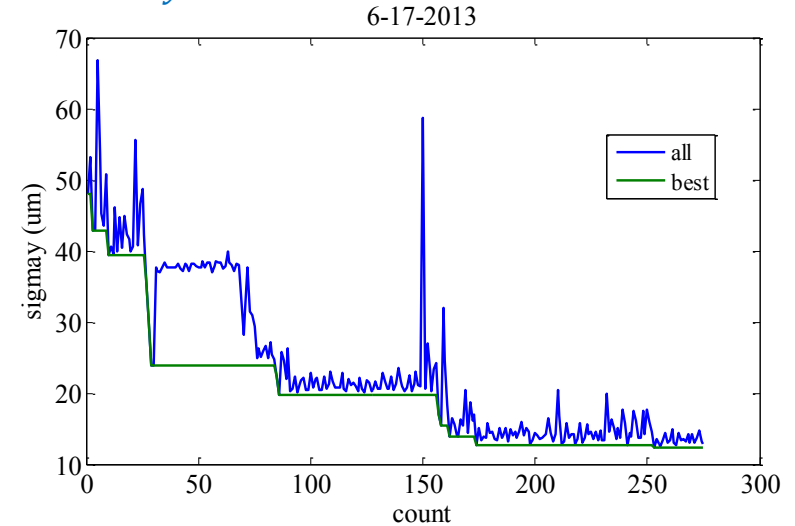
## Using loss rate (normalized) as objective



Beam loss rate is measured by monitoring the beam current change on a 6-second interval (no fitting). Noise sigma 0.04 mA/min. Data were taken at 500 mA with 5-min top-off.

Initially all 13 skew quads were off.  
At 500 mA, the best solution had a lifetime of 4.6 hrs. This was better than the LOCO correction (5.2 hrs)

## Using $\sigma_y$ from pinhole camera as objective



$\sigma_y$  noise level at 0.3 micron.  
All 13 skew quads were off initially.

Pinhole camera resolution is limited.

# Applications of RCDS on real-life problems

- SPEAR3

- Kicker bump matching,
- Transport line optics and steering
- Injection efficiency w/ sextupoles

X. Huang, J. Safranek, PRSTAB 18, 084001 (2015)

- LCLS

- Undulator taper optimization

J. Wu, K. Fang, X. Huang, 2014-2016

- BEPC-II luminosity optimization

- Steering and coupling
- Interaction point beta

H. Ji, et al, Chinese Physics C 2015 Vol. 39 (12)

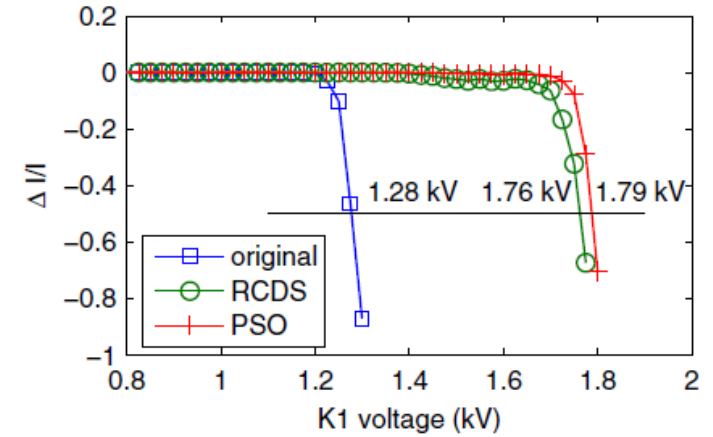
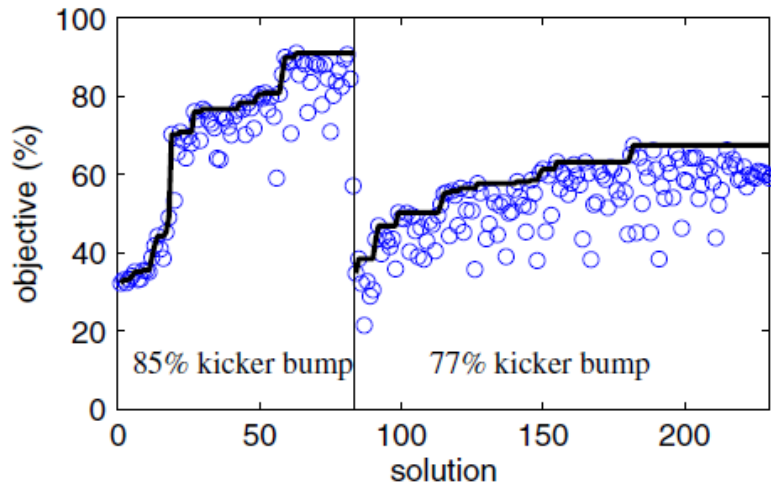
- ESRF

- beam lifetime w/ sextupoles
- Injection steering

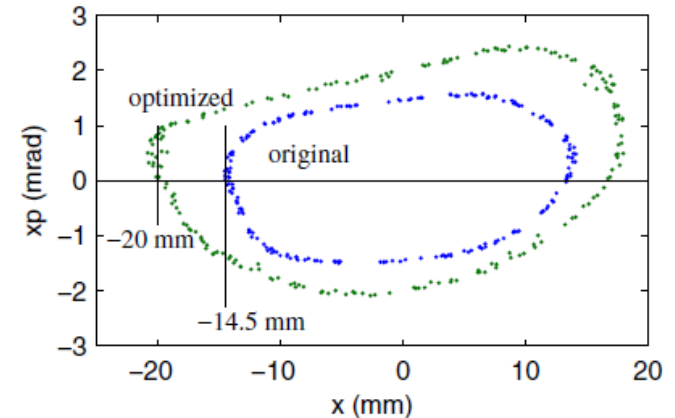
S. M. Liuzzo, et al, IPAC'16, THPMR015

Many other labs successfully applied RCDS in experiments

# Online dynamic aperture optimization for SPEAR3



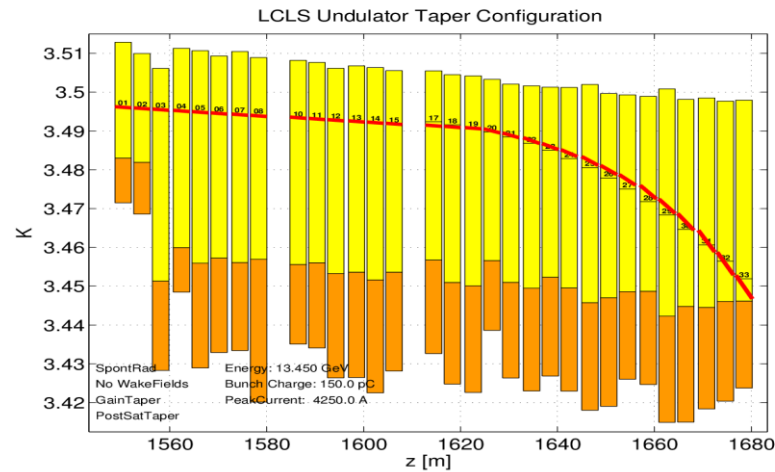
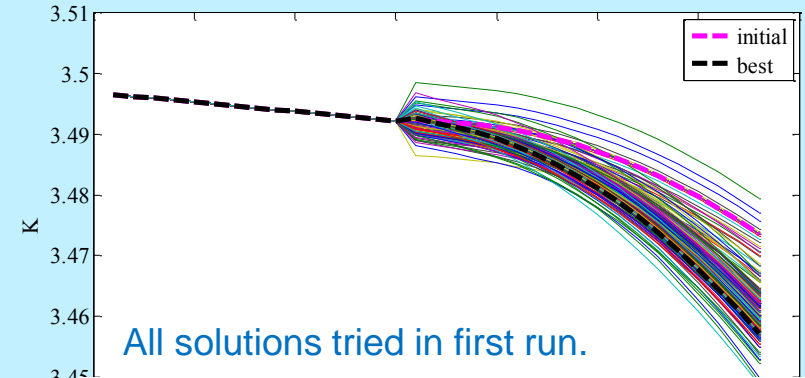
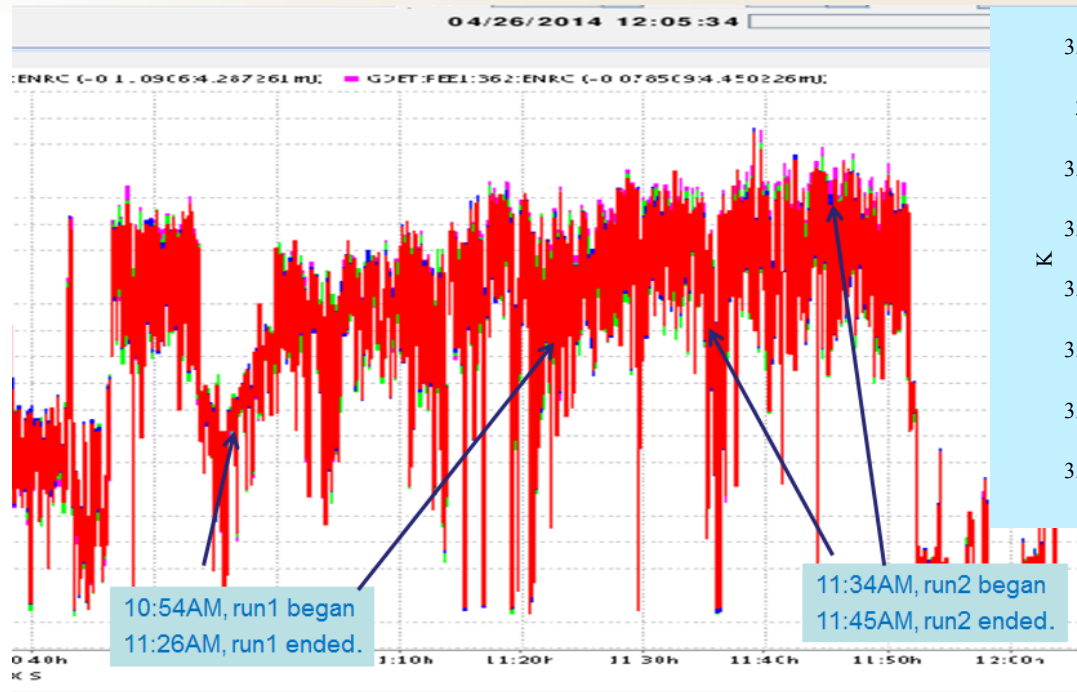
Optimizing injection efficiency with reduced kicker bump.  
Knobs: 8 sextupole knobs – each knob is a pattern of 10 sextupole families that do not change chromaticities.



DA was increased from 15.1 mm to 20.6 mm by optimization. Momentum aperture (MA) was not affected.

X. Huang, J. Safranek, PRSTAB 18, 084001 (2015)

# LCLS taper profile optimization



Knobs: 4 parameters that control the taper profile, two phase shifters.

For U1-U8, and U10-U15:  $K_j = K_0 (1 - a_0 j)$  with  $j = 1, \dots, 15$

For U17-U33:  $K_j = K_1 [1 - a_1 (j - 16) - a_2 (j - z_2)^2]$  with  $j = 17, \dots, 33$ .

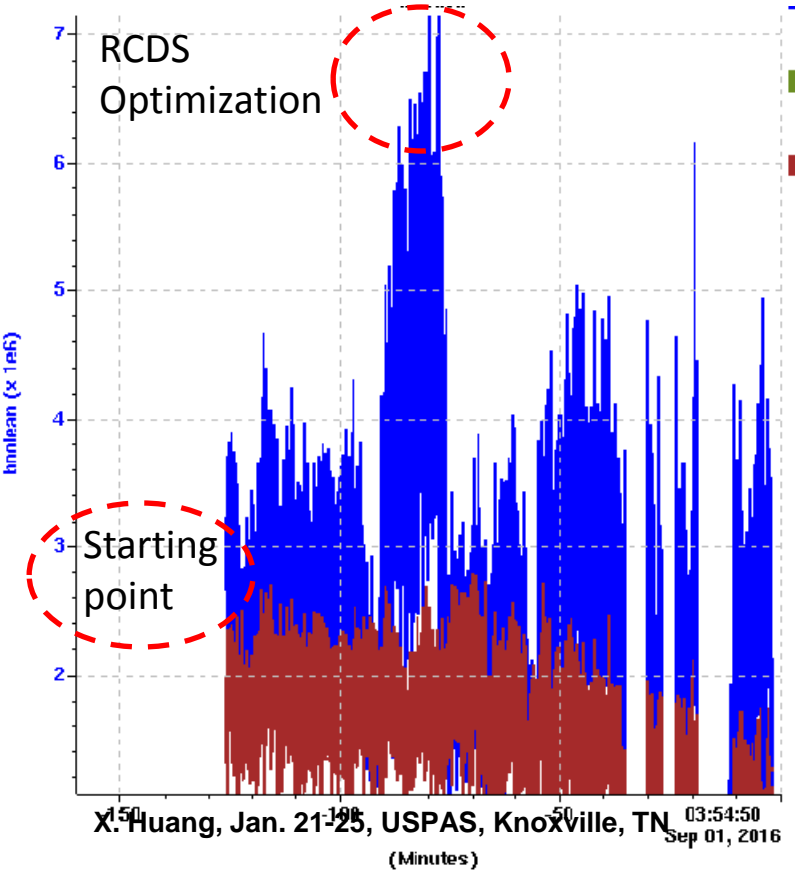
Objective: FEL photon beam intensity.

J. Wu, K. Fang, X. Huang, 2014

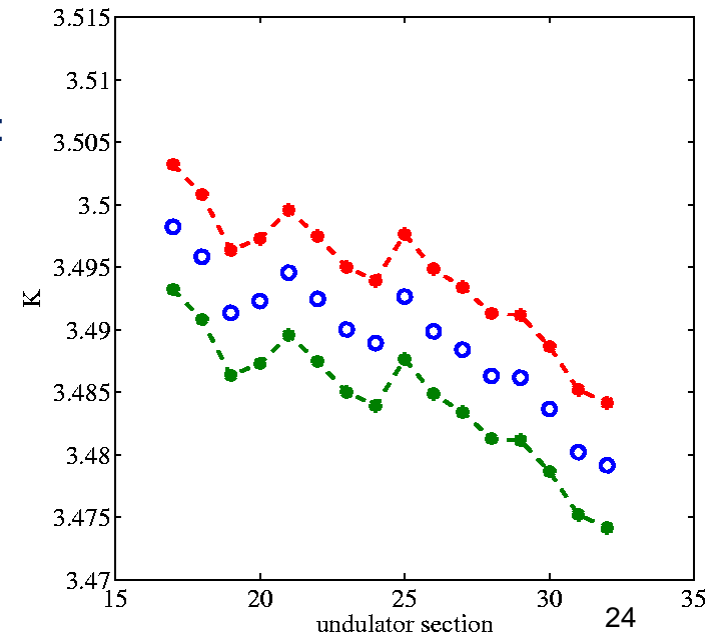
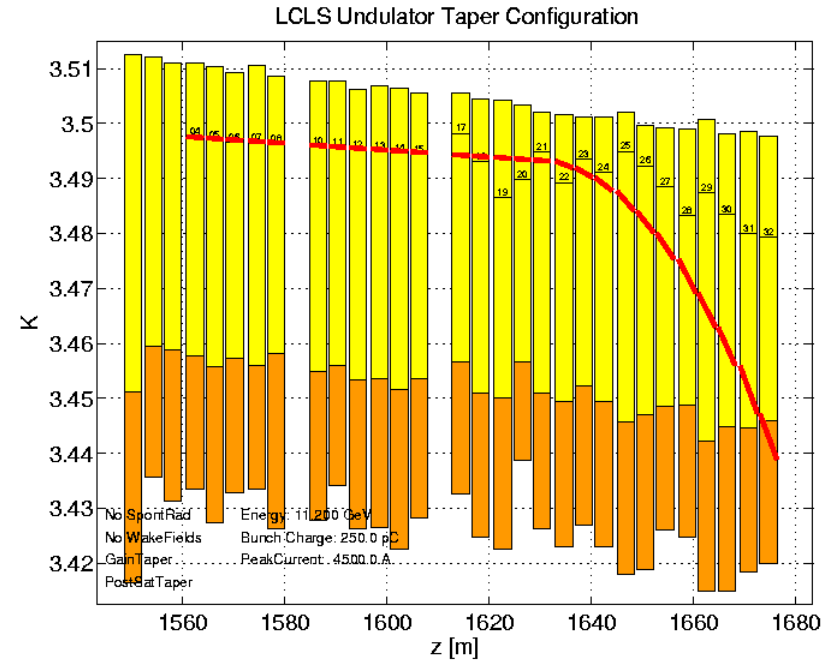
# SELF-SEEDING FEL OPTIMIZATION

## 5.5 KeV Self-seeding FEL

- More than doubled
- U17-U32 continuous function: does **not** work well
- Zig-zag taper profile:  $\sim 1$  mJ in 10 fs

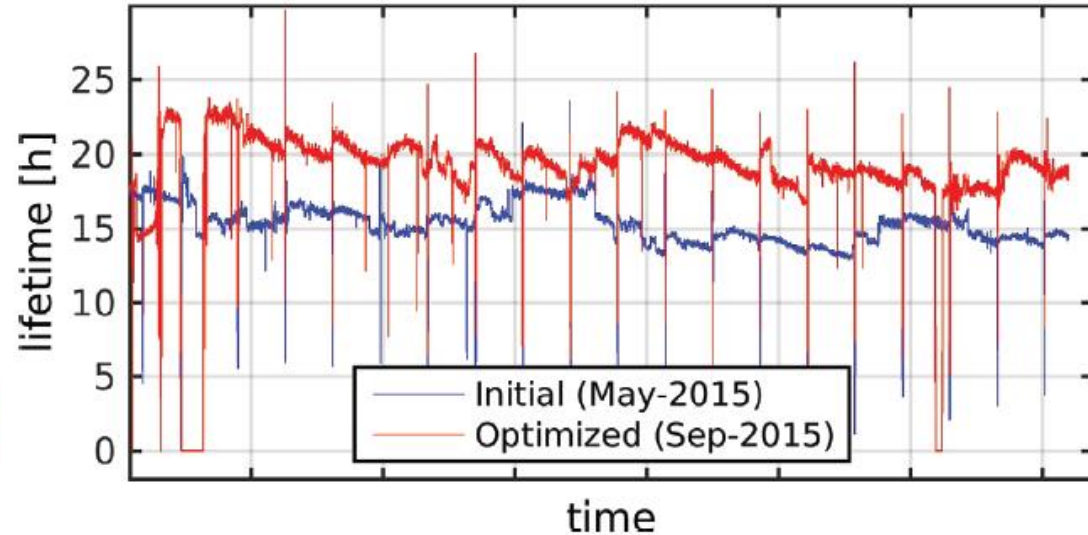
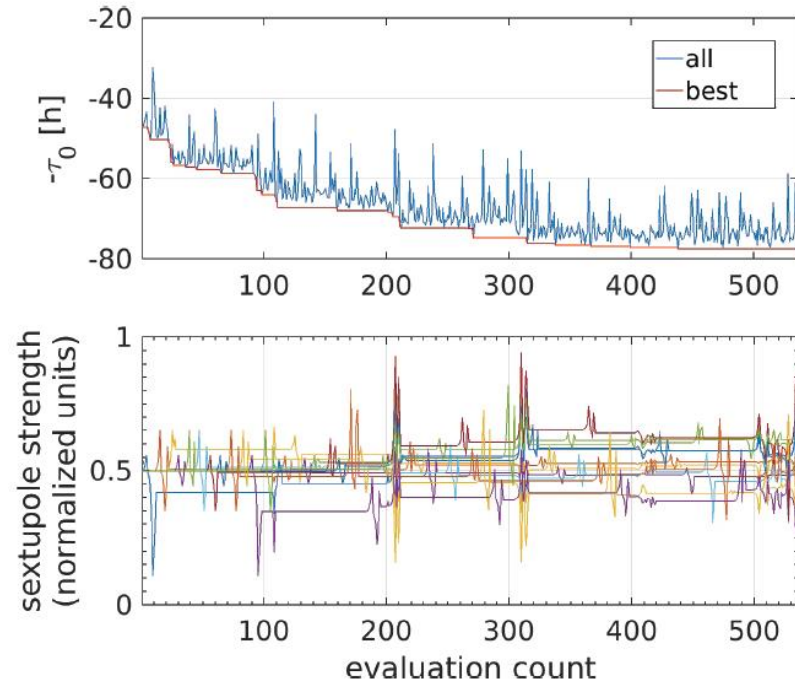


Knobs: 16 parameters that control the taper profile. For U17-U32: *each  $K$  is freely optimized with bounds.* Objective: FEL photon beam intensity.





# ESRF optimization of beam lifetime with sextupoles



Lifetime for the 16-bunch mode in one month before and after optimization.

Figure 2: Optimization of lifetime using 12 sextupole correctors in 7/8+1 mode.

Objective: lifetime normalized by current, bunch length, and vertical size (average over 13 beam size monitors)

$$\tau_0 = \tau \frac{I}{I_0} \frac{BL(I_0)}{BL(I)} \frac{\sigma_{y,0}}{\sigma_y}$$

S. M. Liuzzo, et al, IPAC'16, THPMR015

# The usage of the Matlab RCDS code

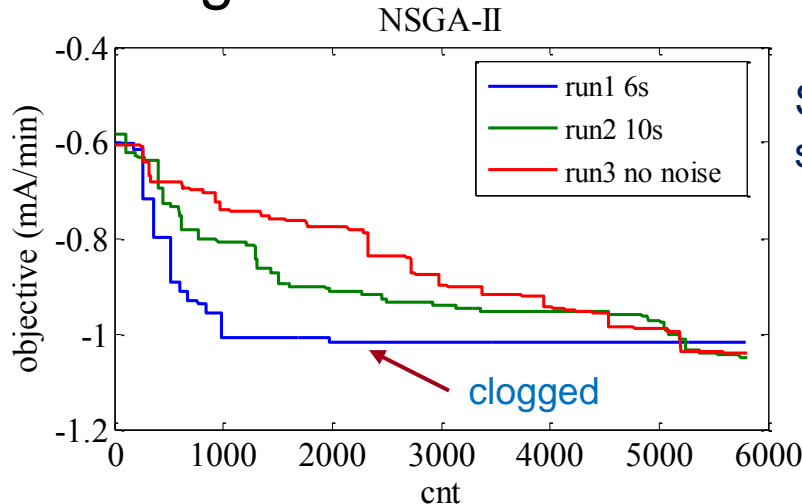
- A Matlab RCDS package is available, with instructions and examples. [A Python version has also been developed and is available.](#)
- The setup for a new problem is extremely simple:
  - Modify an objective function template
    - Make changes to knobs and take measurement of performance
    - Record data
  - Modify a setup and launch script
    - House keeping: record initial parameters, set parameter ranges
    - Measure and specify noise level (only needed once)
    - Launch RCDS
    - Sort solutions and apply the best solution.

This test was performed very rapidly thanks to the clear and user friendly implementation of the RCDS Matlab code. --- S. M. Liuzzo, et al, IPAC'16

- RCDS is not simply a variation of Powell's method
  - Yes, RCDS is implemented as Powell's method with the new robust line optimizer.
  - But in online application one seldom benefits from conjugate direction update because only limited directions are replaced.
  - It is the **robust line optimizer** that gives rise to the effectiveness of RCDS.
- RCDS is not simple iterative parameter scan
  - It works with combined knobs.
  - Parameter scan usually have fixed scan ranges and pre-determined, uniform step sizes. Choice of step size (or # of steps) is problem dependent.
  - RCDS uses bracketing, variable step size, and quadratic fitting – a lot more efficient.
  - RCDS algorithm does not need problem-dependent setup.

# Genetic algorithm (NSGA-II)

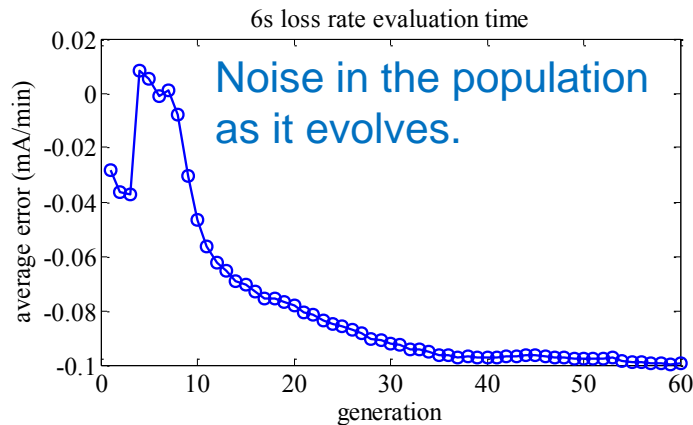
- Genetic algorithm is inefficient even without noise.



Same SPEAR3 coupling correction simulation problem.

Population: 100; Ran 60 generations; 10% mutation, 90% crossover.

- Noise gives a bias to the selection operation.



Bad guys (solutions with favorable random errors) tend to enter the next generation. This prevents converging to the true minimum.

X. Huang et al, Nucl. Instr. Methods, A 726 (2013) 77-83.

# Particle swarm optimization

- In PSO a solution is considered as a particle in the parameter space. The algorithm manipulates a group of solutions (fixed number) over many iterations
  - The solutions are updated by adding a velocity term, which is given by the past velocity, its distance to the best solution in its trajectory, and the distance to an overall best solution.

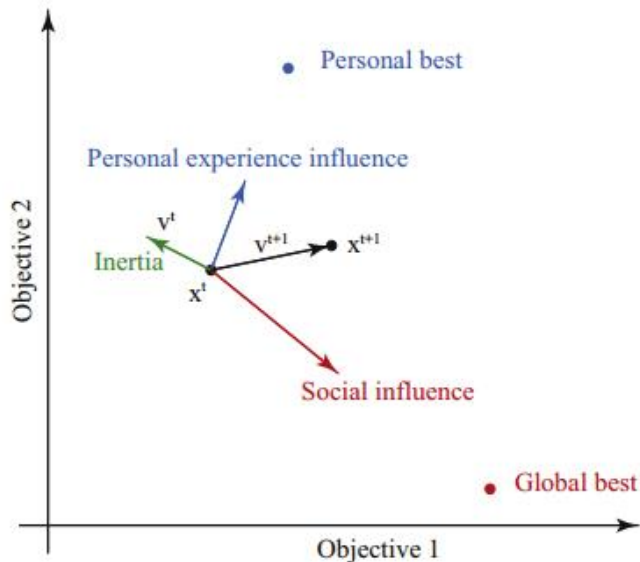


Fig. 1. Velocity and position updates in PSO.

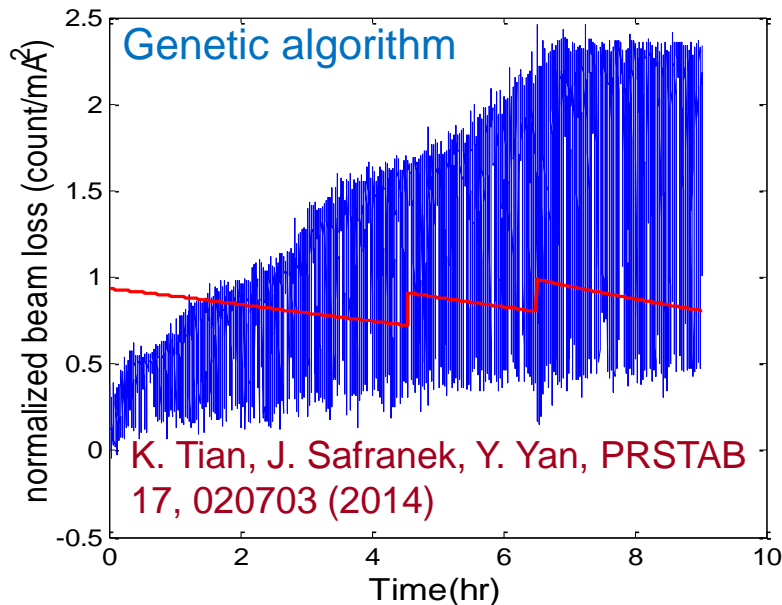
$$\mathbf{x}_i^{t+1} = \mathbf{x}_i^t + \mathbf{v}_i^{t+1}$$

$$\mathbf{v}_i^{t+1} = w\mathbf{v}_i^t + c_1r_1(\mathbf{p}_i^t - \mathbf{x}_i^t) + c_2r_2(\mathbf{g}^t - \mathbf{x}_i^t)$$

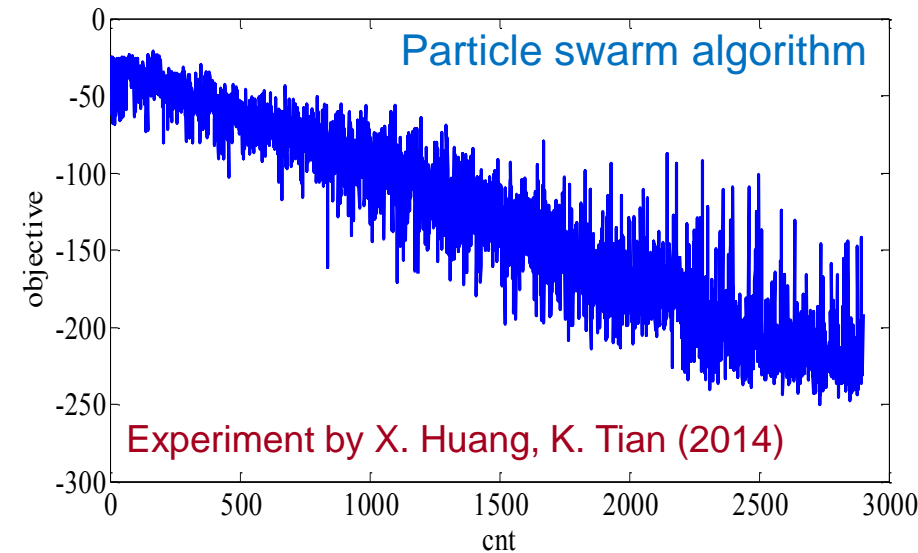
X. Pang, L.J. Rybarczyk, NIMA 741 (2014) 124

# Genetic algorithm and particle swarm algorithm

## Online coupling correction with genetic algorithm



Using beam loss monitor signal (low noise) as objective. It took **20,000** evaluations.



Same setup as the genetic algorithm experiment. It took **3,000** evaluations.

... while RCDS only took **200** evaluations (see slide 17) for a much noisier setup.

When online global search is desired, it seems the particle swarm algorithm is a better choice: (1) more efficient; (2) no bias introduced by noise.

# The Extremum Seeking (ES)\* method

- The ES method cycles parameters

$$p_1(n+1) = p_1(n) + \Delta\sqrt{\alpha\omega_1} \cos(\omega_1\Delta n + k\hat{C}(n))$$

$$p_2(n+1) = p_2(n) + \Delta\sqrt{\alpha\omega_2} \cos(\omega_2\Delta n + k\hat{C}(n))$$

$$\vdots \quad \text{with } \hat{C}(n) = C(\mathbf{p}(n), t) + \nu(t) \leftarrow \text{noise}$$

The optimization parameters (knobs) are rotated with various frequencies and amplitudes, and subject to modulation by the cost function.

At the high frequency limit, the behavior approaches that of a gradient descent method

$$\frac{d\mathbf{p}(t)}{dt} = -\frac{k\alpha}{2} \nabla C^T(\mathbf{p}(t), t)$$

Pros: (1) noise is averaged out; (2) a simple and general framework; (3) can dynamically track the optimum.

Cons: (1) algorithm control parameters are problem specific and need tuning; (2) may not be as efficient as other direct search method (e.g. RCDS, simplex); (3) Parameter update rate is bounded, but parameters are not.

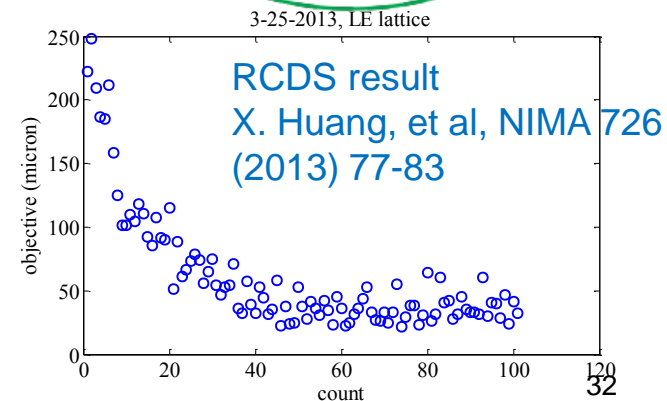
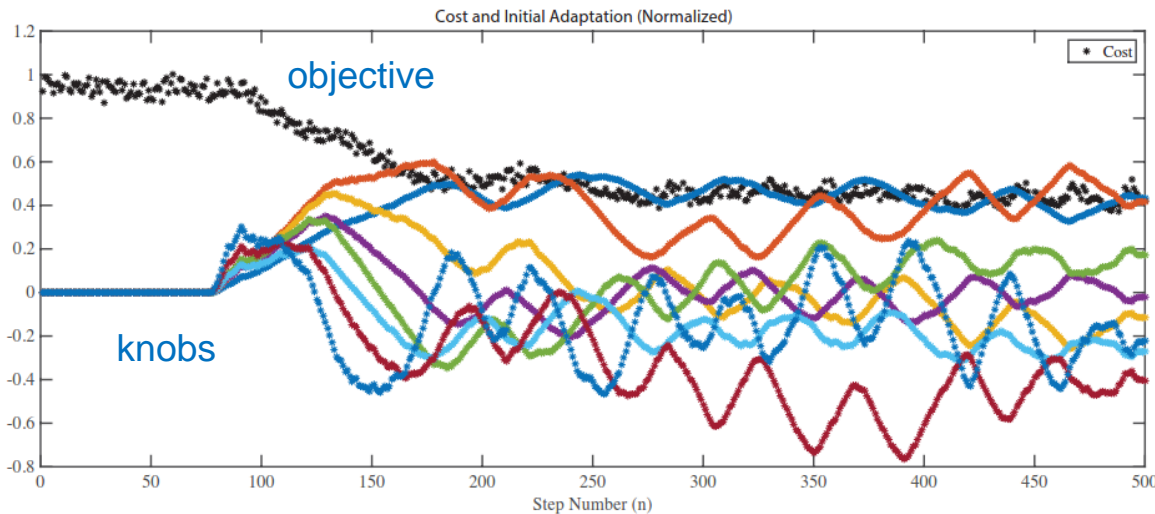
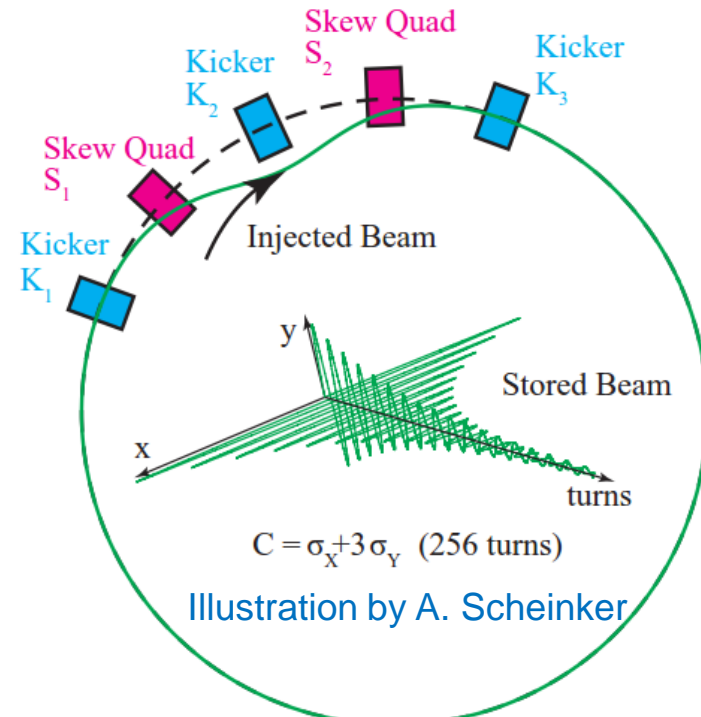
\*A. Scheinker, M. Krstic, IEEE Trans. Automatic Control, 58, 1107 (2013).  
A. Scheinker, M. Krstic, Systems & Control Letters, 63, 25 (2014)

# Test of the ES method on SPEAR3\*

**The problem:** injection kicker bump matching

**Knobs:** pulse amplitude, width, and delay of K1 and K2, and two skew quads – 8 knobs total.

**Objective:** residual oscillation of stored beam

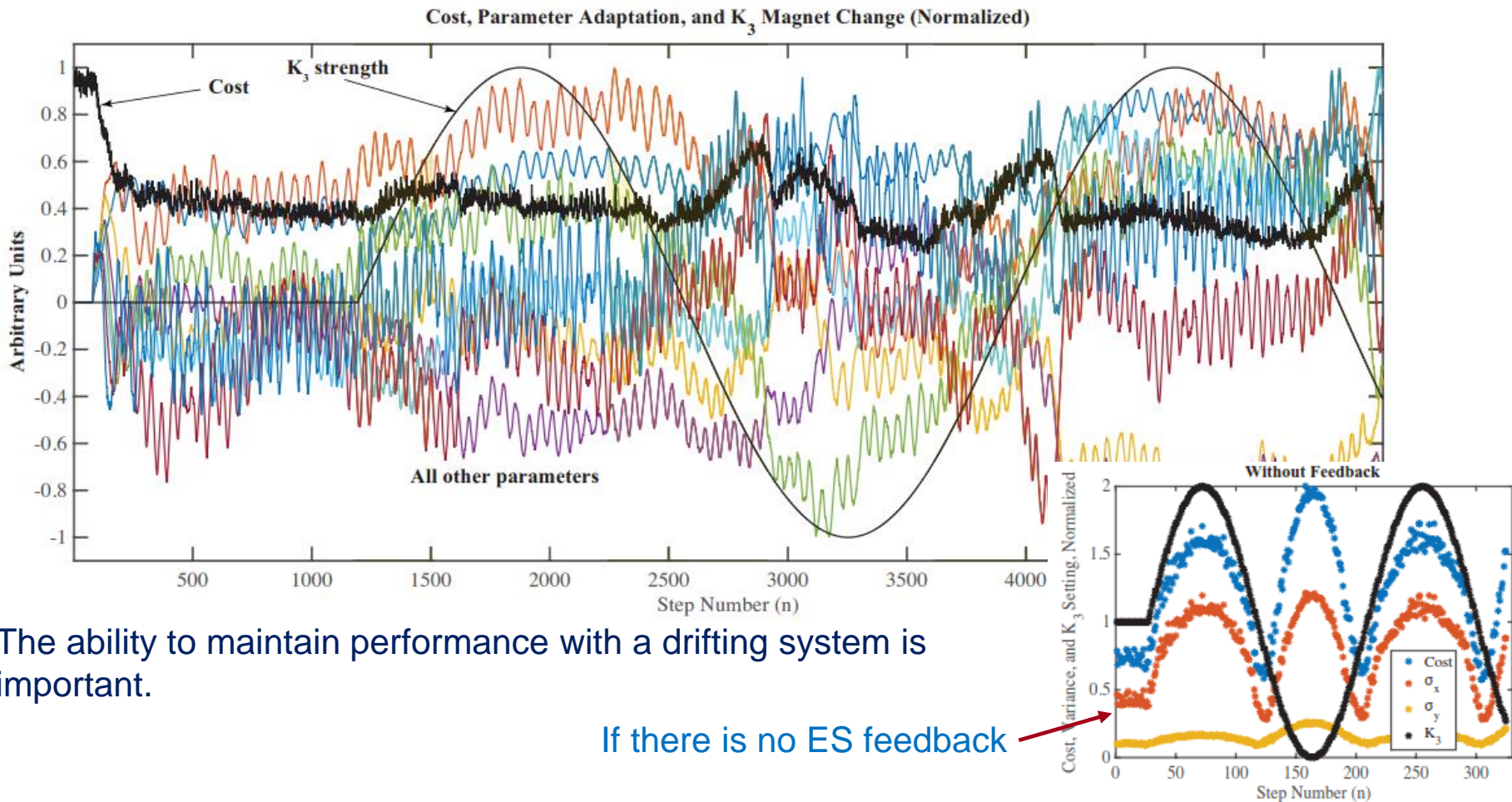


\*A. Scheinker, X. Huang, J. Wu, SLAC-PUB-16508 (2016)



# ES – dynamic tracking of the objective

In this test one parameter ( $K_3$  voltage, not an optimization variable) is varied, while the ES algorithm serves as a feedback to make compensation.



The ability to maintain performance with a drifting system is important.

If there is no ES feedback

# Bayesian optimization

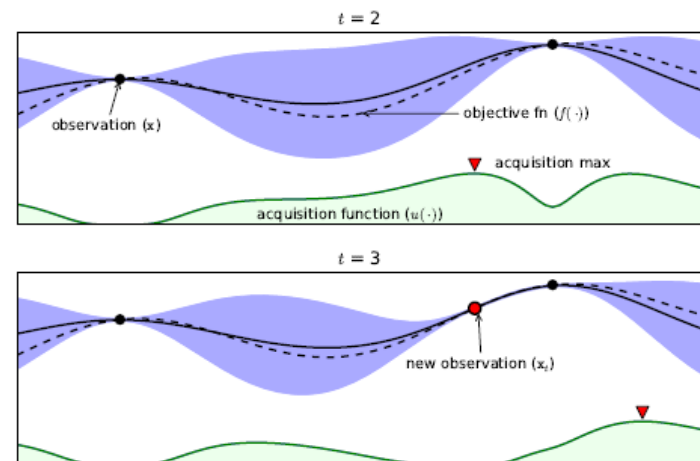
- Bayesian optimization: use measured data and assumed prior probability model and to construct a posterior probability model of the objective function, which is then used to guide further parameter space exploration.

Bayes's theorem  $P(M|E) \propto P(E|M)P(M)$  M: prior probability  
P(E|M): probability of E under condition M

- Based on the posterior model (“surrogate function”), an acquisition function is defined. The next sampling point is decided by maximizing (or minimizing) the acquisition function.

The acquisition function should strike a balance between exploitation and exploration.  
Example:  $\mu + \kappa\sigma$  (upper confidence bound)

E. Brochu, v. M. Cora, N. de Freitas, “A tutorial on Bayesian optimization of ...”, arXiv:1012.2599 (2010)



# Bayesian optimization with Gaussian process

- A Gaussian process (GP) can serve as the prior model of objective function

- GP is the Gaussian random distribution of functions which is given by the mean function and the covariance function

$$f(\mathbf{x}) \sim \mathcal{GP}(m(\mathbf{x}), k(\mathbf{x}, \mathbf{x}'))$$

Often assumed:  $m(\mathbf{x}) = 0$ ,

$$k(\mathbf{x}, \mathbf{x}') = \exp\left(-\frac{1}{2} \|(\mathbf{x} - \mathbf{x}')\boldsymbol{\theta}^{-2}(\mathbf{x} - \mathbf{x}')^T\|\right).$$

- The posterior model

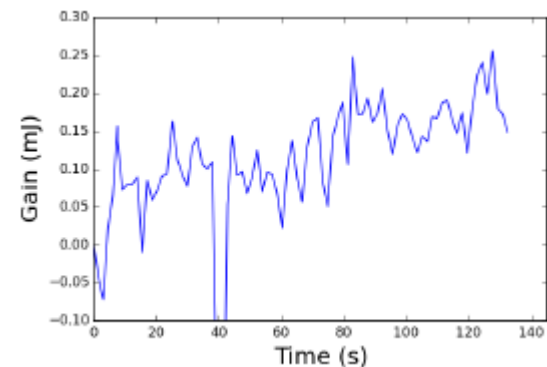
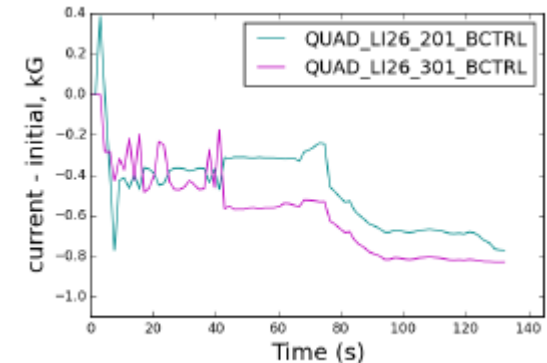
$$P(f_{t+1} | \mathcal{D}_{1:t}, \mathbf{x}_{t+1}) = \mathcal{N}(\mu_t(\mathbf{x}_{t+1}), \sigma_t^2(\mathbf{x}_{t+1}))$$

with

$$\begin{aligned} \mu_t(\mathbf{x}_{t+1}) &= \mathbf{k}^T \mathbf{K}^{-1} \mathbf{f}_{1:t} \\ \sigma_t^2(\mathbf{x}_{t+1}) &= k(\mathbf{x}_{t+1}, \mathbf{x}_{t+1}) - \mathbf{k}^T \mathbf{K}^{-1} \mathbf{k} \end{aligned}$$

Kernel matrix

$$\mathbf{K} = \begin{bmatrix} k(\mathbf{x}_1, \mathbf{x}_1) & \dots & k(\mathbf{x}_1, \mathbf{x}_t) \\ \vdots & \ddots & \vdots \\ k(\mathbf{x}_t, \mathbf{x}_1) & \dots & k(\mathbf{x}_t, \mathbf{x}_t) \end{bmatrix} \quad \mathbf{k} = [k(\mathbf{x}_{t+1}, \mathbf{x}_1) \quad k(\mathbf{x}_{t+1}, \mathbf{x}_2) \quad \dots \quad k(\mathbf{x}_{t+1}, \mathbf{x}_t)]$$



Gaussian process optimization has been used on LCLS  
M. McIntire, et al, IPAC 2016; J. Duris, et al, HB2018

# Summary

- Computer controlled systems can be optimized online without a model or knowledge of system interior.
- Online optimization is challenging for algorithms due to noise and parameter space complexity
- There are several algorithms workable for online optimization
  - The RCDS algorithm is a robust and efficient method for online optimization, tested on many accelerator problems.
- This is a fast developing area.