



**USPAS 2015: East Brunswick, Rutgers**

**Closed Orbit Stability, Correction  
and Feedback**

***Christoph Steier***

**Lawrence Berkeley National Laboratory**

# Outline

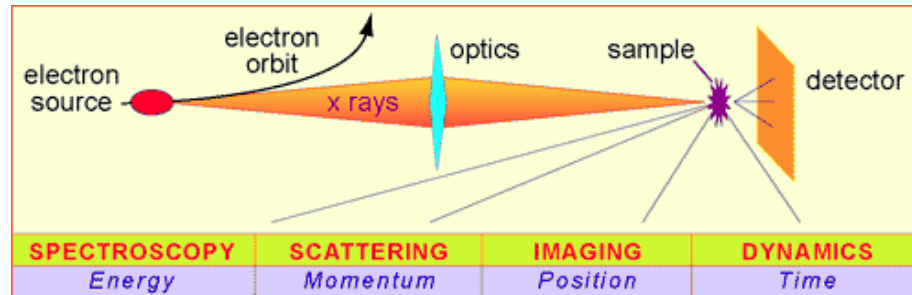
- Introduction/Motivation
- Measurement Methods/BPMs
- Sources of Orbit Noise/Drift
- Orbit Correction/Feedback
  - Correction Algorithms
  - Feedback Systems (Slow, RF, Fast)
- Beam Based Alignment

# Motivation

Orbit stability is one of the most important requirement in accelerators

- There are many reasons why good orbit stability is necessary
- Accelerator Physics:
  - Spurious effects (dispersion, coupling, beta beating) due to off center trajectories in magnets
  - Equipment protection
  - Beam-beam overlap at interaction point.
- Users:
  - Stability of photon source point
  - Stability of interaction point in colliders.

# Beam Stability: Requirements



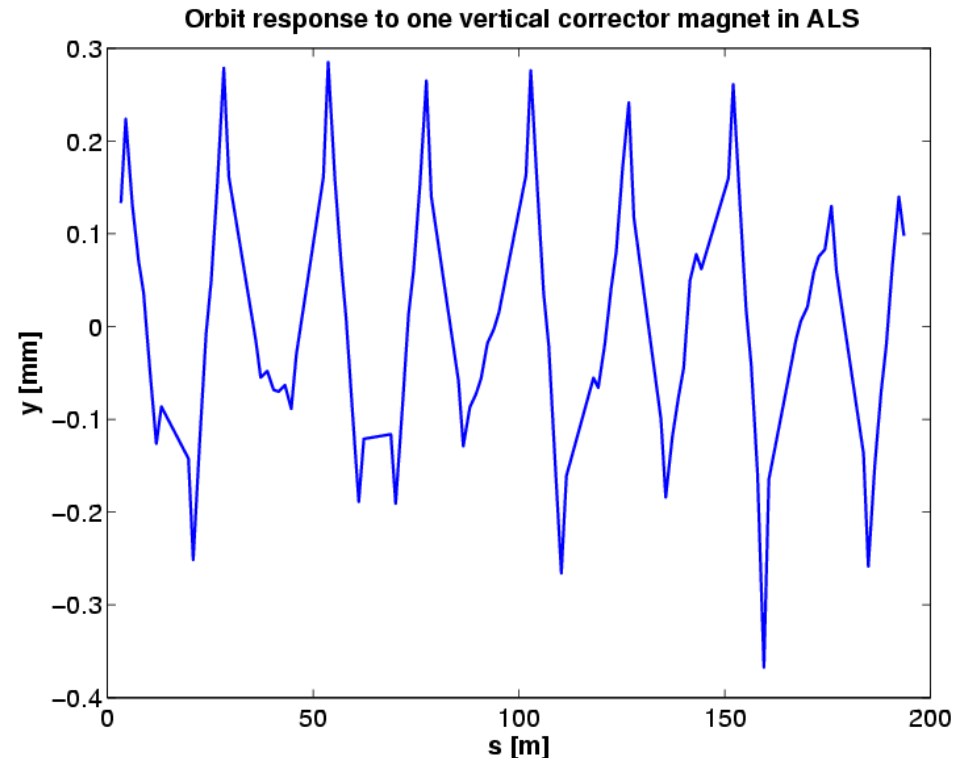
## Typical requirements of modern SR user experiments:

Measurement parameter	Stability Requirement
Intensity variation $\Delta I/I$	$\ll 1\%$ of normalized $I$
Position and angle	$< 2\text{-}5\%$ of beam $\sigma$ and $\sigma'$
Energy resolution $\Delta E/E$	$< 10^{-4}$
Timing jitter	$< 10\%$ of critical time scale
Data acquisition rate	$10^{-3} - 10^5$ Hz

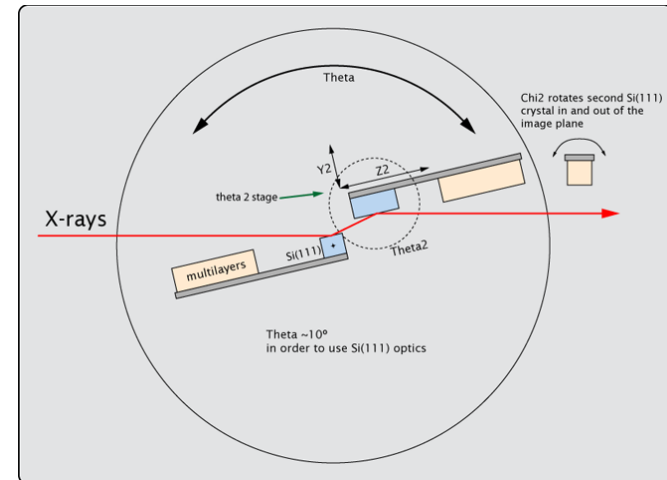
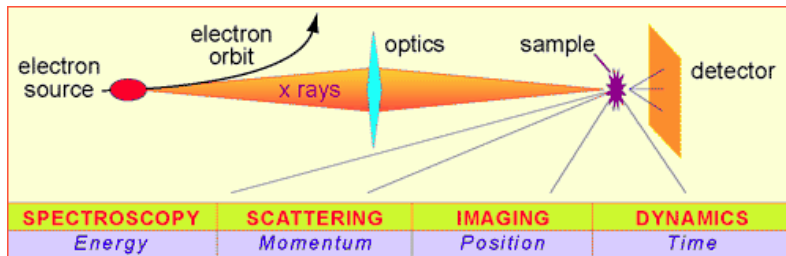
- All of those requirements relate back into stability requirements for beam position + angle, beamsize + emittance, beam energy, beam energy spread, ...
- Often stability can be more important to SR users than brightness+flux
- For current SR sources, this means for example submicron orbit stability (for ERLs in both planes)

# Closed Orbit: 'Definition'

- ❑ The closed orbit is the (periodic) particle trajectory which closes after one turn around the machine (in position and angle) i.e. the fixed point in 4 (6) dimensional space for the one-turn map.
- ❑ The ideal orbit is the orbit through the centers of all (perfectly) aligned magnetic elements.
- ❑ Particles close to the closed orbit will oscillate around it.



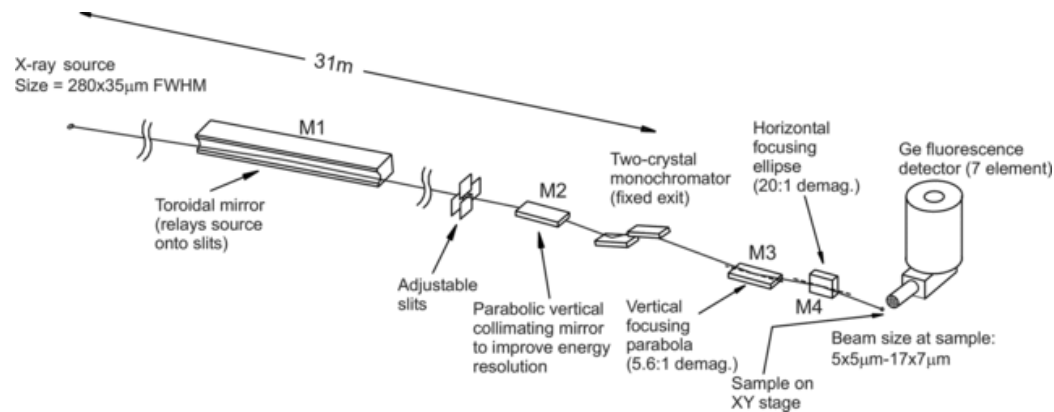
# Why does the orbit/position need to be constant



- Without slits it is obvious that beam motion will translate to motion of photon beam on sample, i.e. different sample areas are measured
- Similarly in a monochromator without slits a vertical beam motion translates into a photon energy shift
- With slits, the effects get smaller and smaller with smaller slit size (there still are 2<sup>nd</sup> order effects because of the beam profile and the nonzero slit size). However, the smaller the slit the smaller the transmission and the larger the intensity fluctuations (and effects of slit alignment and motion).

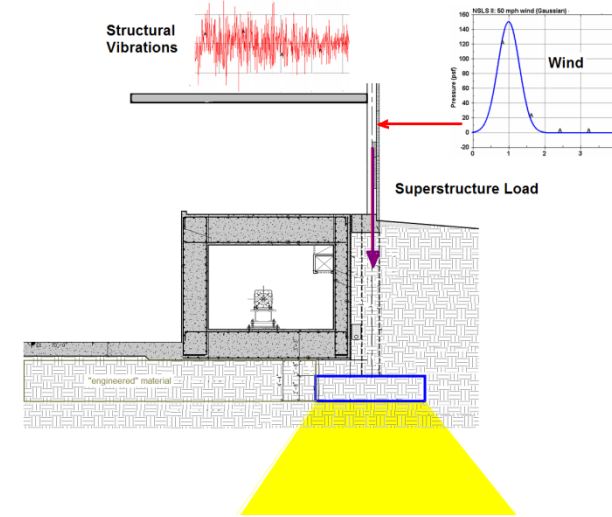
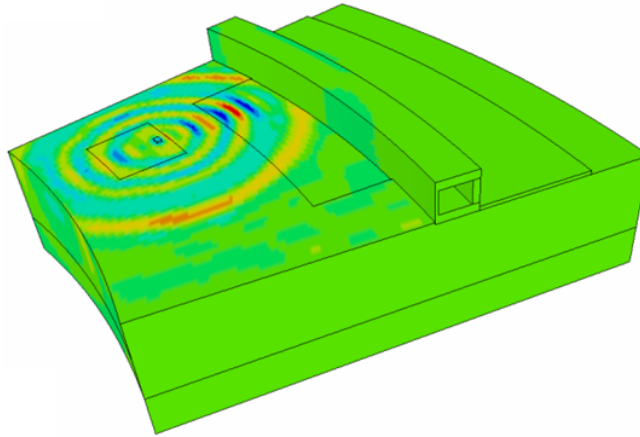
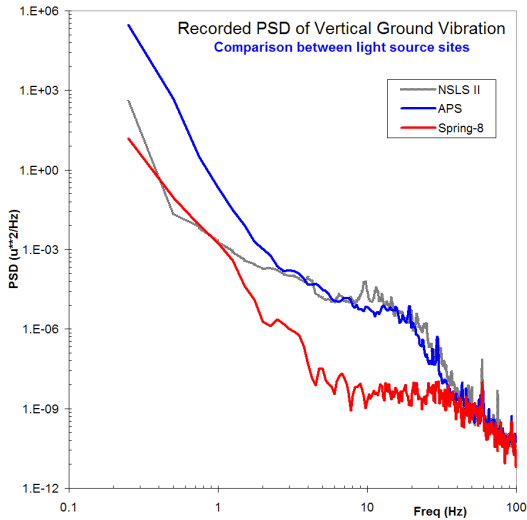
# Actual Beamline Example

- Beamline 10.3.2 at the ALS
- Hard x-ray, microfocus, micro X-ray absorption or fluorescence, ...
- Environmental samples ( 'dirt' )
- Very heterogenous



The image cannot be displayed. Your computer may not have enough memory to open the image, or the image may have been corrupted. Restart your computer, and then open the file again. If the red x still appears, you may have to delete the image and then insert it again.

# Stability / Design

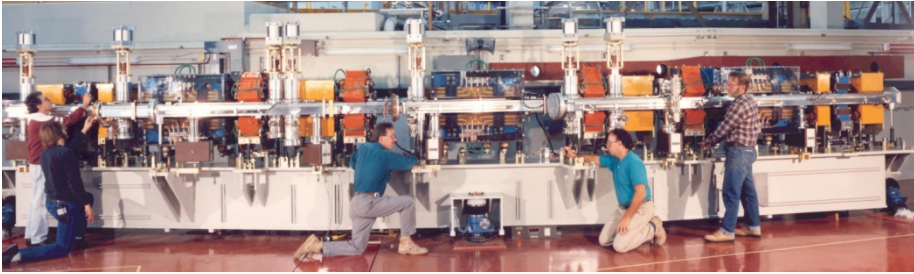


Courtesy: N. Simos,  
NLSL-II

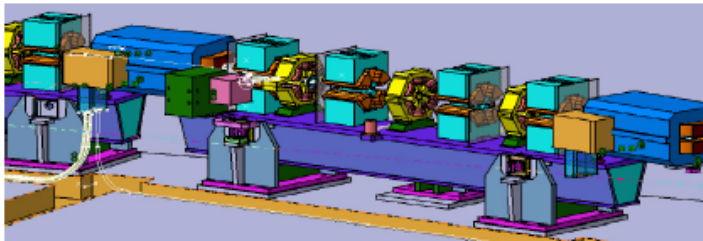
- One hopefully starts by selecting a good / quiet site (not always possible) - at least need to know all caveats
- Nowadays FEA allows optimization of slab design
- Important: Minimize vibration coupling from pumps, ...
- Also keep external disturbances in mind (wind, sun, ...)



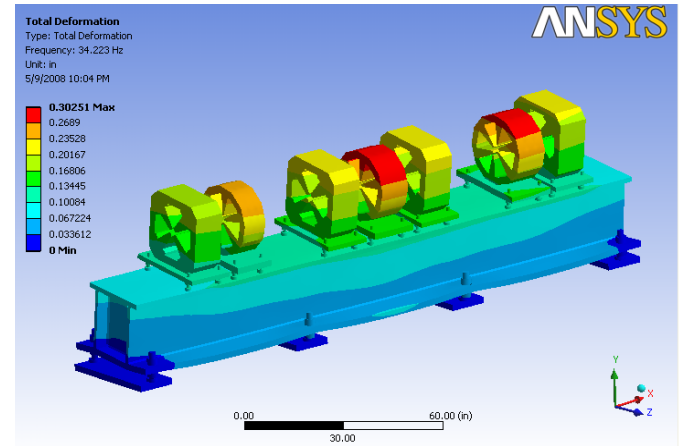
# Girder Design



ALS



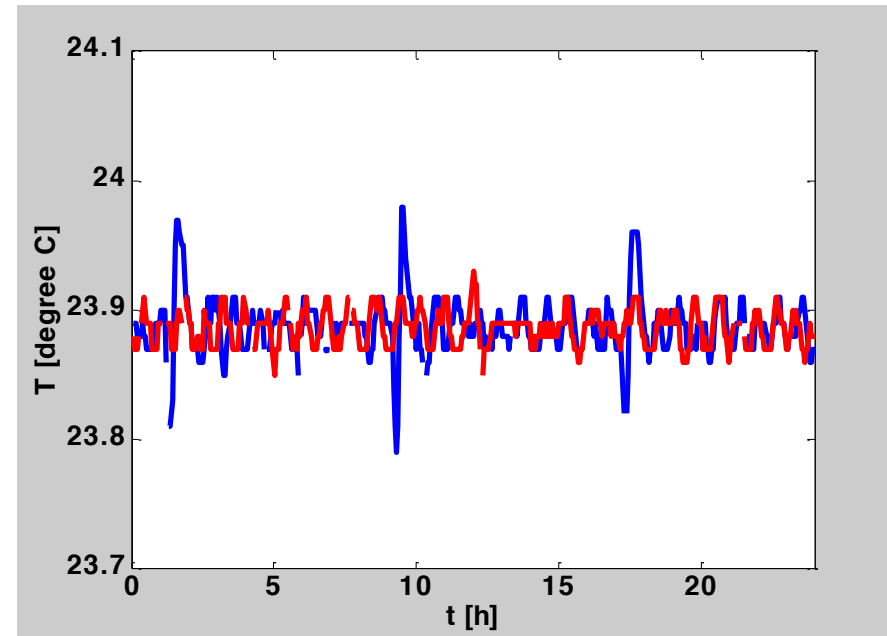
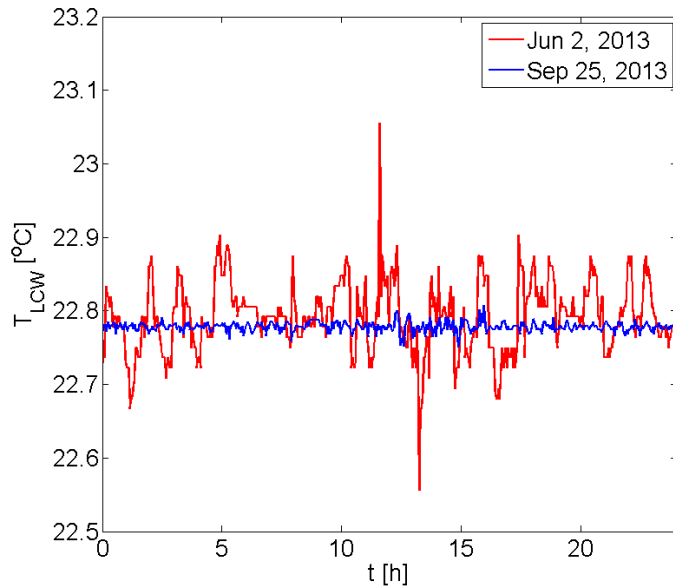
Soleil



NSLS-II: courtesy S. Sharma

- Some early 3<sup>rd</sup> generation sources had massive girders (low resonance frequencies – sampling larger ground oscillation amplitudes)
- Later ones had girders with higher resonance frequencies but movers, that significantly lowered them
- Latest designs (Soleil, NSLS-II) avoid this caveat – smaller vibration transmission to beam

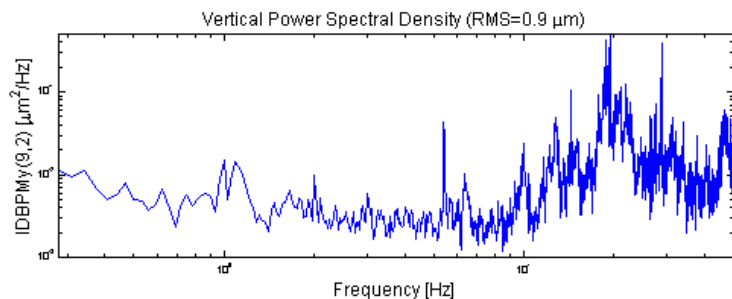
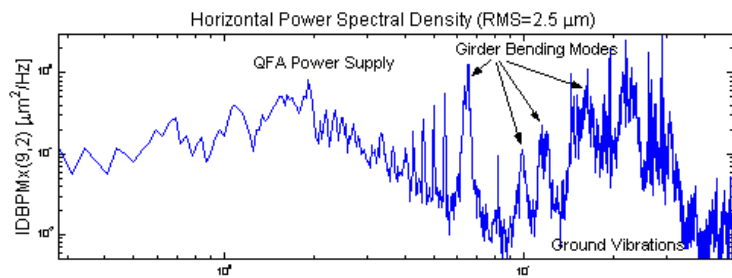
# Air/water temperature stability



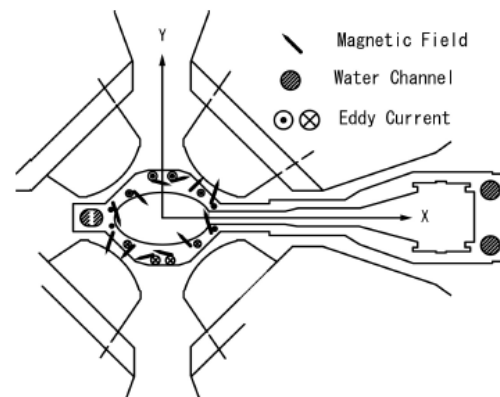
Left: ALS water temperature, Right: Tunnel air temperature

- Stable environmental conditions are extremely important
- State of the art is water and tunnel air temperature stability on the order of 0.1 degree C
- Stable power supply controllers, invar rods for BPM mounts, ... also help, but it is always best to also keep the conditions constant

# Identify and Fix Problems



Data taken on 12-12-1999, during a 1.9 GeV user run at 278 mAmps



**Eddy Current made  
by Q-mag. field kicks  
the electron beam.**

S. Matsui, et al. *Jpn. J. Appl. Phys.*  
Vol. 42 (2003) pp.L338

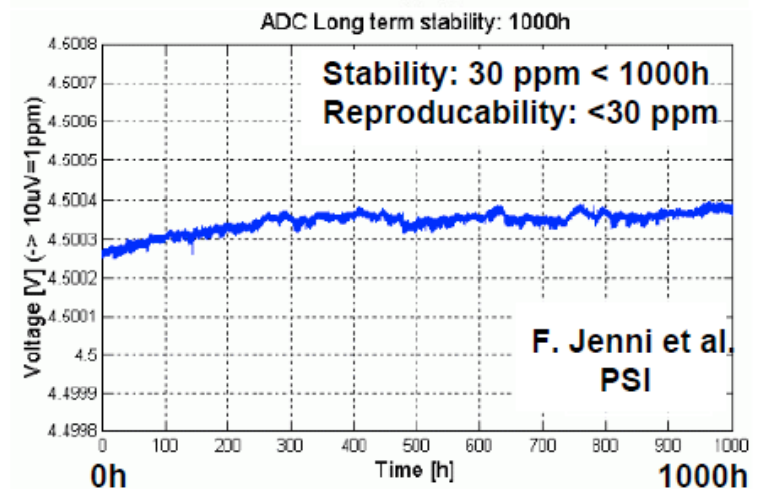
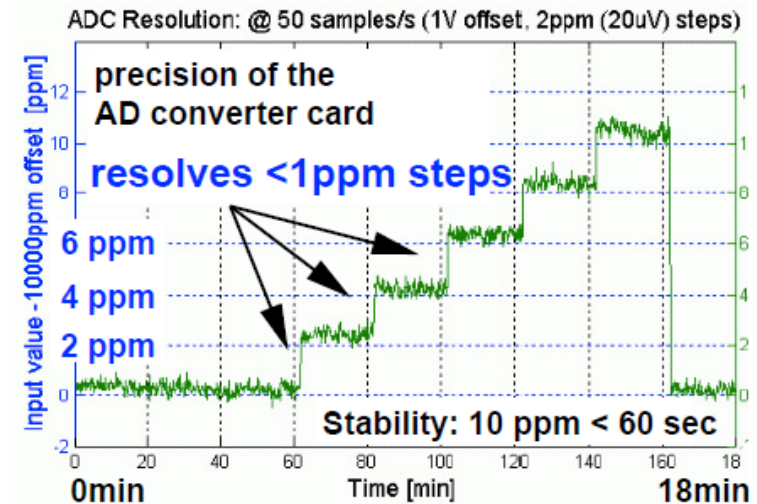
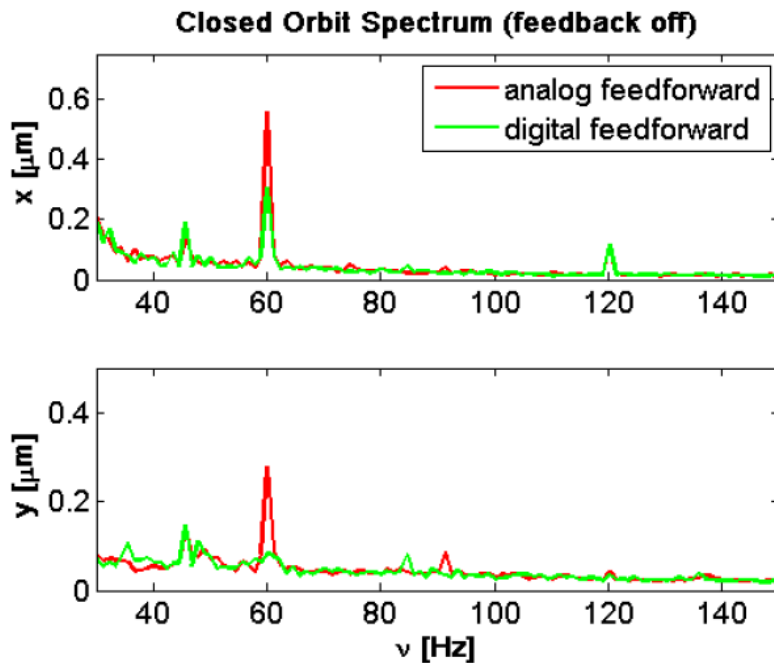
ALS – fixed power supply

Spring-8: water vibration

- Often vibration sources / coupling into sensitive equipment is found during after commissioning
- Fixing the worst offenders often gives big benefit
- Examples above: Power supply at ALS, water induced vacuum chamber vibration at Spring-8; Another example are viscoelastic damping elements at ESRF

# Good power supplies are essential

- Strong corrector magnets with high vacuum chamber cut off frequencies can be significant sources of orbit noise
- Observed at several light sources
- Achievable power supply performance increased over the years



# Closed orbit errors

- A single dipole error will create an orbit distortion which looks very simple in normalized coordinates:

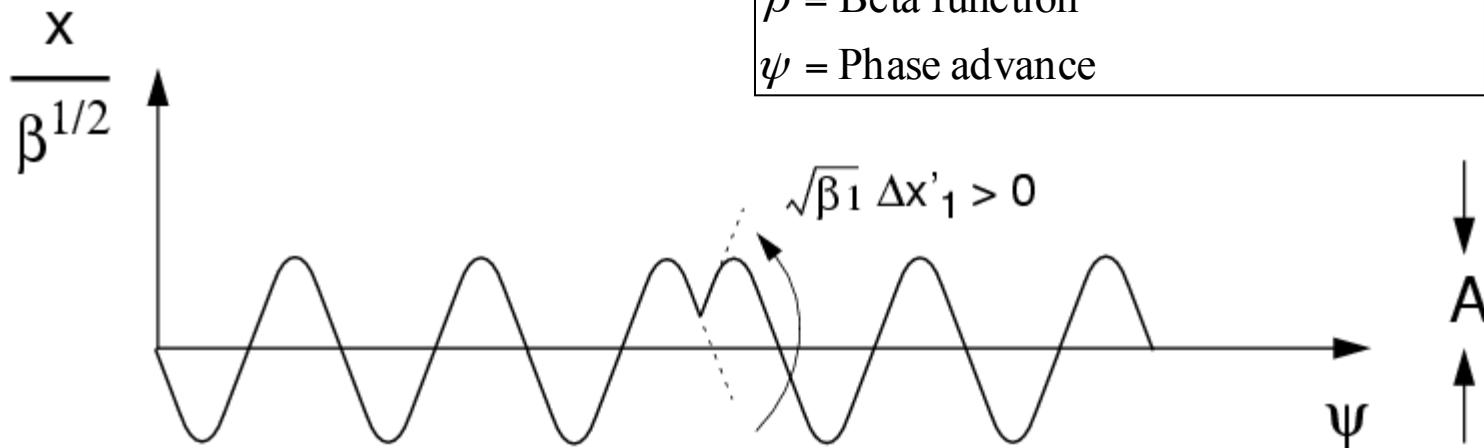
$$x(s) = \Delta x' \frac{\sqrt{\beta(s)\beta_0}}{2 \sin \pi\nu} \cos(|\psi(s) - \psi_0| - \pi\nu)$$

$\Delta x$  = Transverse position

$\Delta x'$  = Kick strength [radians]

$\beta$  = Beta function

$\psi$  = Phase advance

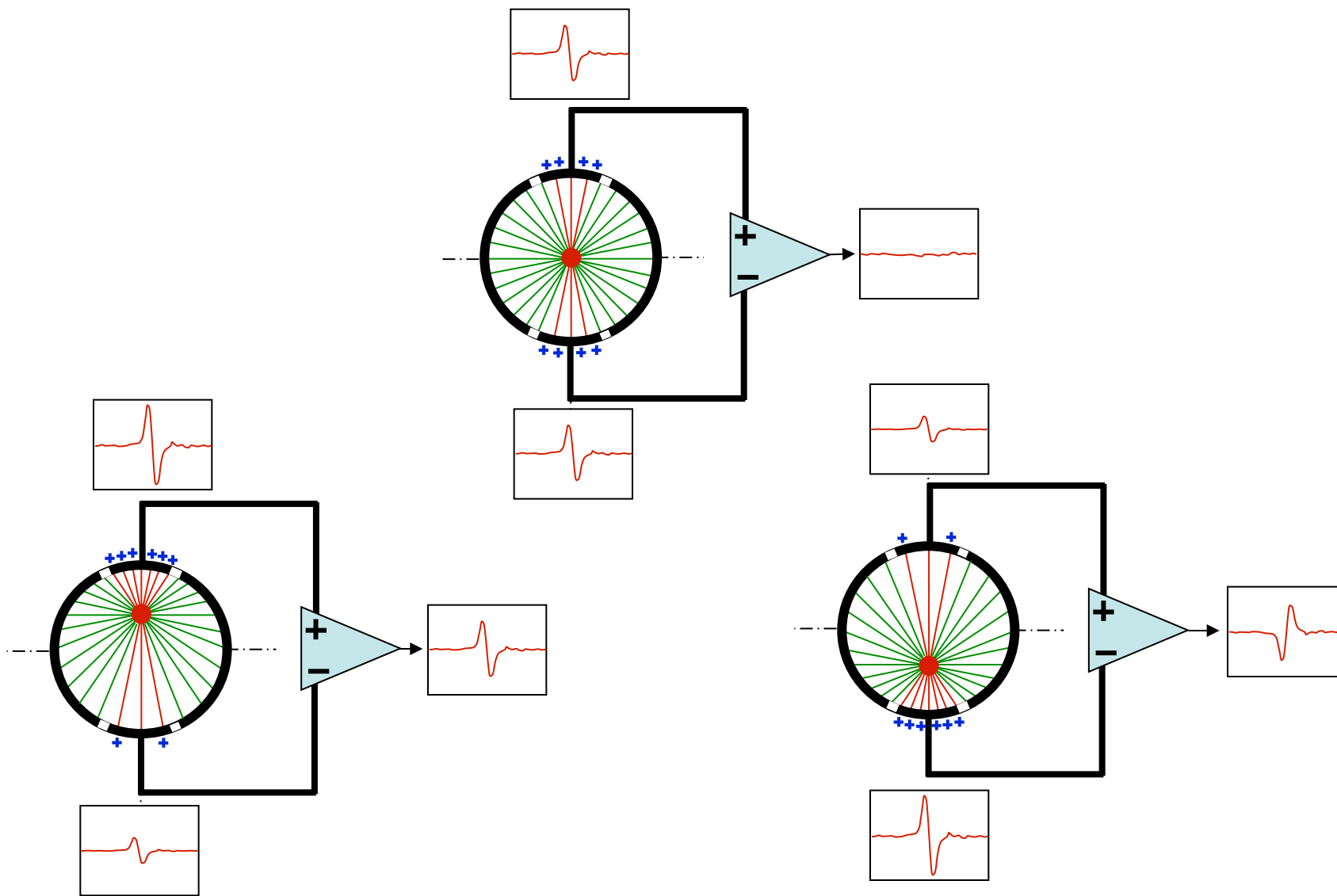


The matrix containing the change in position at every BPM to a kick from every corrector magnet is called orbit response matrix (used in orbit correction). For an uncoupled machine it can be calculated (linear approximation) using above formula.

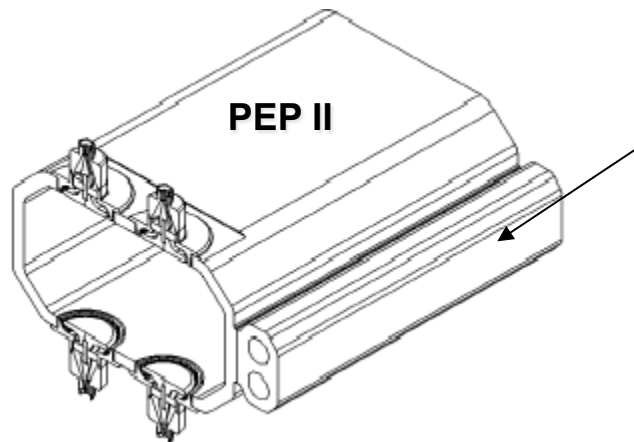
# Orbit Measurement Methods

- Main categories are:
  - Destructive/non destructive measurements
  - RF/synchrotron radiation/scattering/absorbing based detection
  - Pure position/profile measurements
  - Fast/Slow (GHz-mHz)
- Linear accelerators and beamlines often use very different methods from storage rings
- Lepton accelerators often use methods different from hadron accelerators

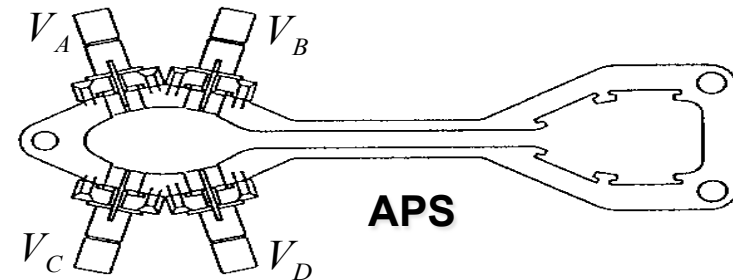
# Electromagnetic Beam Position Monitors



# Capacitive Pickups

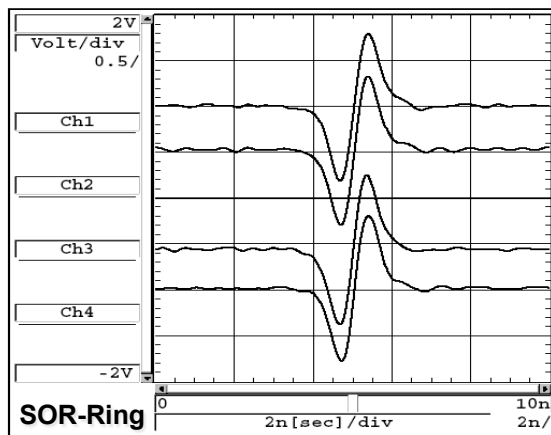


• Typical geometry used in the presence of synchrotron radiation.



$$\Delta x = K \frac{(V_A + V_C) - (V_B + V_D)}{V_A + V_B + V_C + V_D}, \quad \Delta y = K \frac{(V_A + V_B) - (V_C + V_D)}{V_A + V_B + V_C + V_D}$$

• Capacitive type (derivative response), low coupling impedance, relatively low sensitivity, best for storage rings.





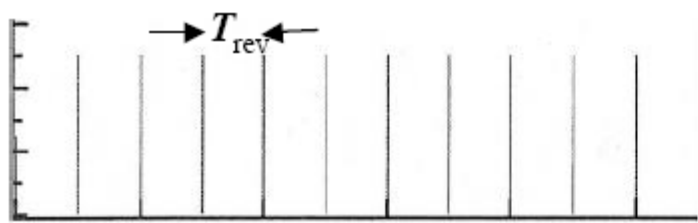
# Bunch spectrum

Using a spectrum analyzer with a BPM can yield a wealth of information on beam optics and stability. A single bunch with charge  $q$  in a storage ring with a revolution time  $T_{\text{rev}}$  gives the following signal on an oscilloscope

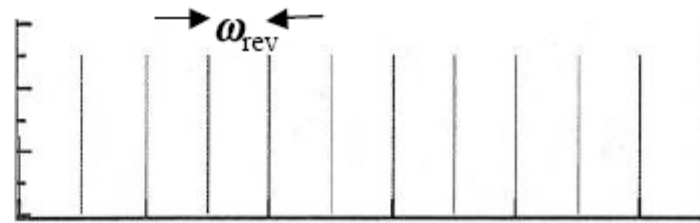
$$I(t) = \sum_{n=-\infty}^{\infty} q \delta(t - nT_{\text{rev}}),$$

where I'm assuming a zero-length bunch. A spectrum analyzer would see the Fourier transform of this,

$$I(\omega) = \sum_{n=-\infty}^{\infty} q \omega_{\text{rev}} \delta(\omega - n\omega_{\text{rev}})$$



Time

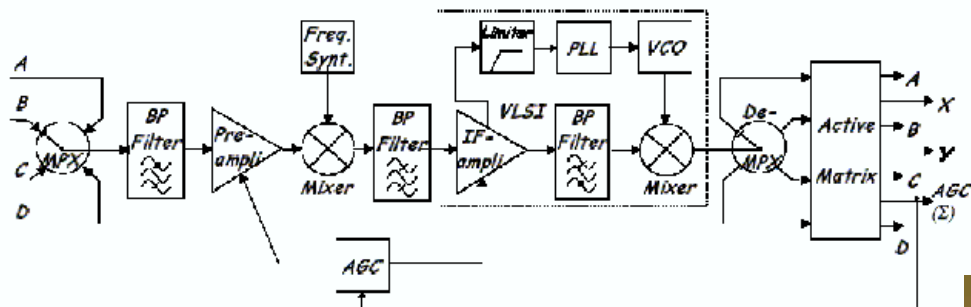


Frequency

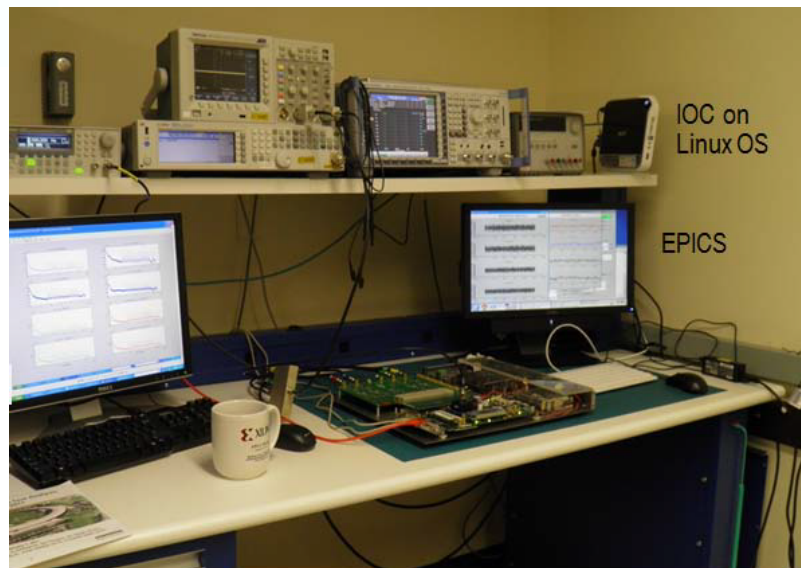
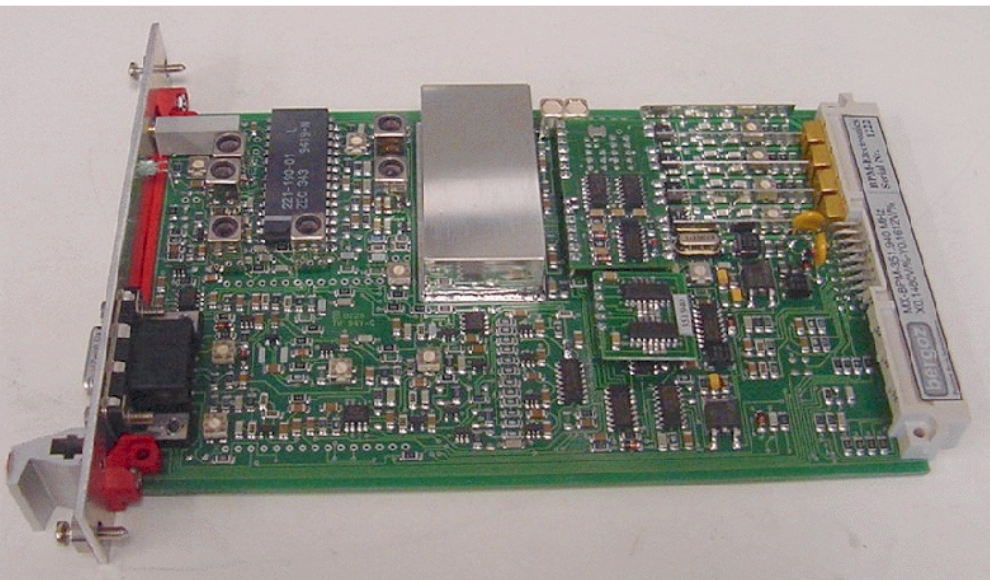
# Signal Processing Electronics

Bittner / Biscardi / Galayda / Hinkson/ Unser / Bergoz Narrowband Receiver

Normalization accomplished via multiplexing plus automatic gain control (AGC)\*:



- More recently: Digital BPMs only frontend is analog, followed by ADCs, FPGAs (sometimes DSP) and digital signal processing



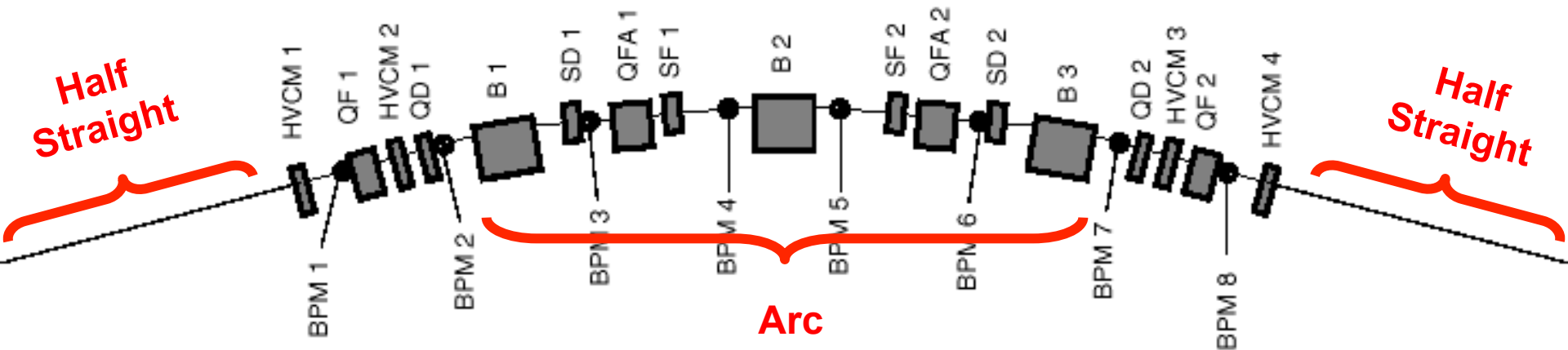
Courtesy Kurt Vetter

# Aerial view of the Advanced Light Source

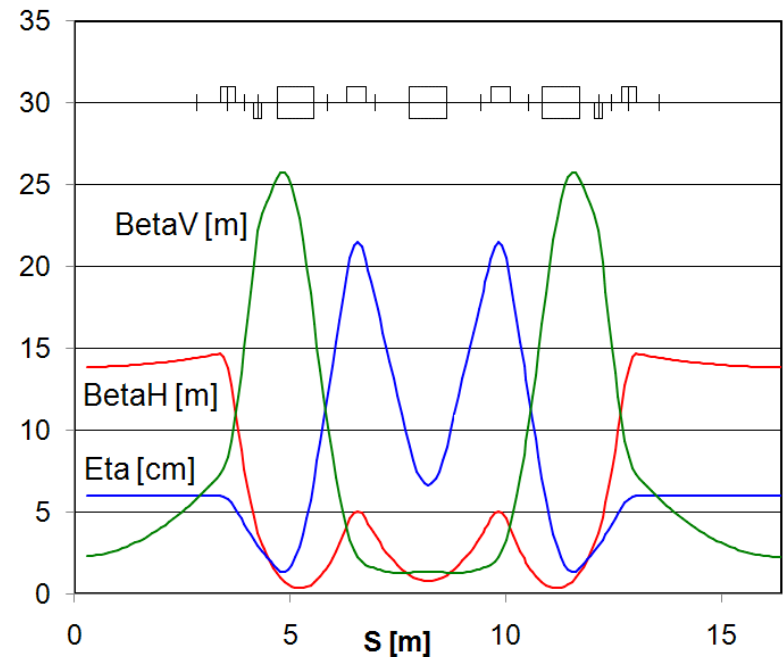


jc/ALSaerial/11-96

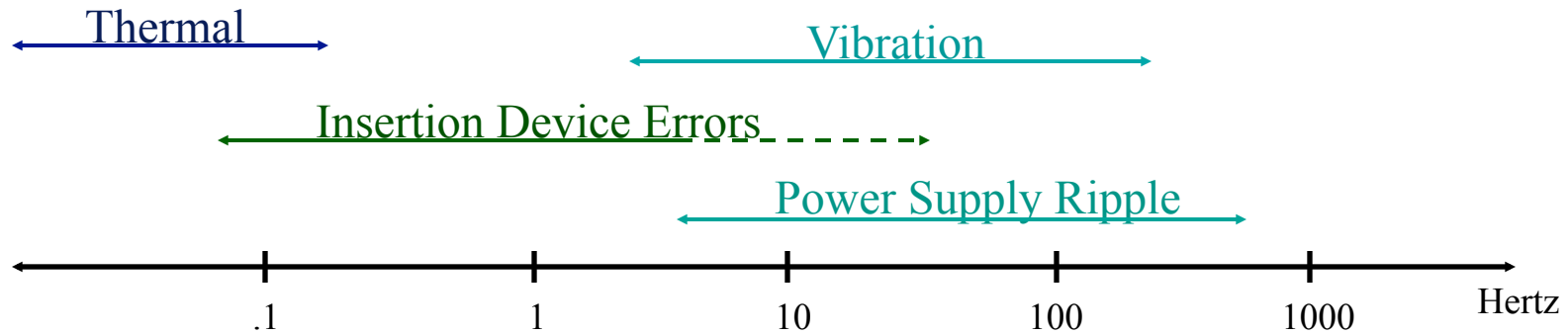
## ALS – orbit measurement + correction



- 12 nearly identical arcs – TBA; aluminum vacuum chamber
- 122 beam position monitors in each plane (about 4 of stable type per arc)
- 8 horizontal, 6 vertical corrector magnets per arc (94/70 total)
- 24 individual skew quadrupoles
- beam based alignment capability in all quadrupoles (either individual power supplies or shunts)
- 22 corrector magnets in each plane on especially thin vacuum chamber pieces



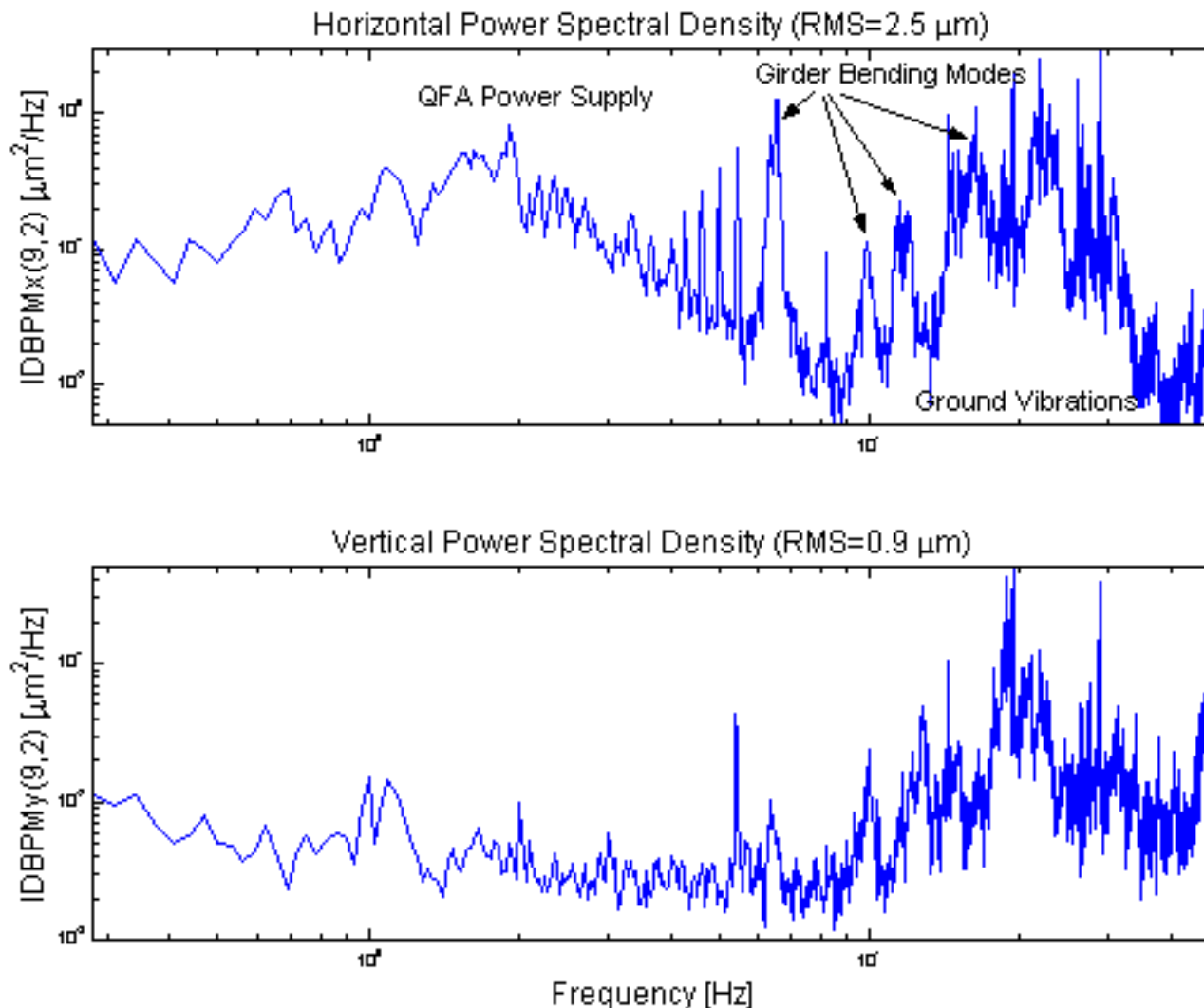
# Causes for Orbit Distortions



Frequency	Magnitude	Dominant Cause
Two weeks (A typical experimental run)	$\pm 200 \mu\text{m}$ Horizontal $\pm 100 \mu\text{m}$ Vertical	<ol style="list-style-type: none"> <li>1. Magnet hysteresis</li> <li>2. Temperature fluctuations</li> <li>3. Component heating between 1.5 GeV and 1.9 GeV</li> </ol>
1 Day	$\pm 125 \mu\text{m}$ Horizontal $\pm 50 \mu\text{m}$ Vertical	Temperature fluctuations
8 Hour Fill	$\pm 50 \mu\text{m}$ Horizontal $\pm 20 \mu\text{m}$ Vertical	<ol style="list-style-type: none"> <li>1. Temperature fluctuations</li> <li>2. Feed forward errors</li> </ol>
Minutes	1 to 5 $\mu\text{m}$	<ol style="list-style-type: none"> <li>1. Feed forward errors</li> <li>2. D/A converter digitization noise</li> </ol>
.1 to 300 Hz	3 $\mu\text{m}$ Horizontal 1 $\mu\text{m}$ Vertical	<ol style="list-style-type: none"> <li>1. Ground vibrations</li> <li>2. Cooling water vibrations</li> <li>3. Power supply ripple</li> <li>4. Feed forward errors</li> </ol>

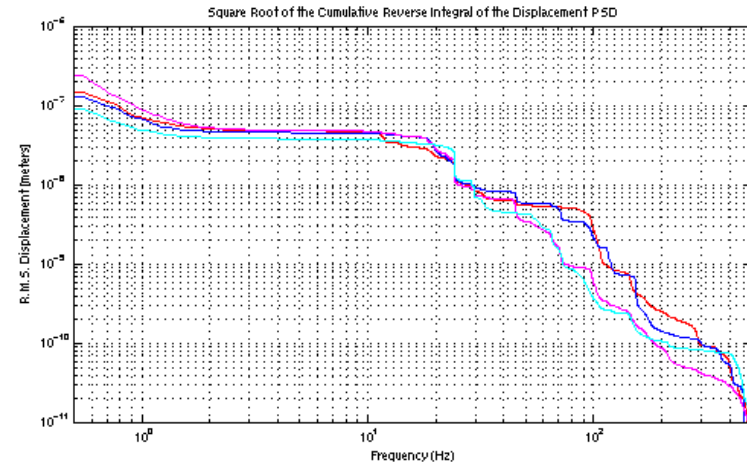
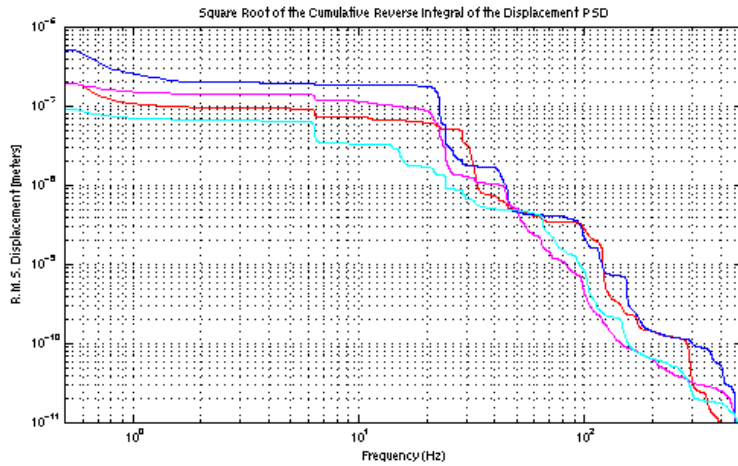
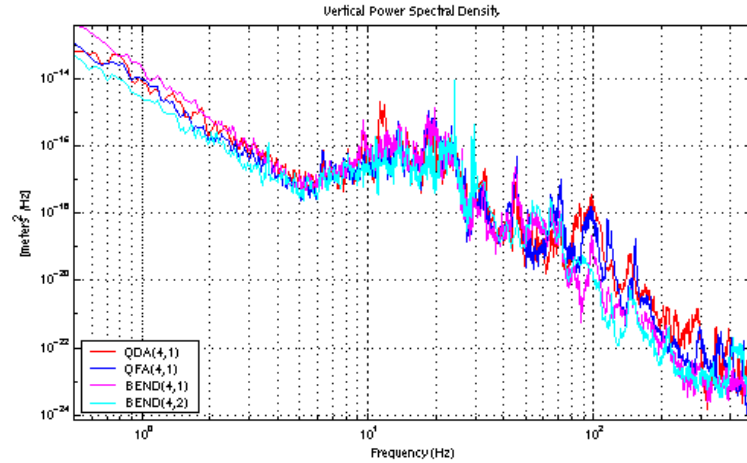
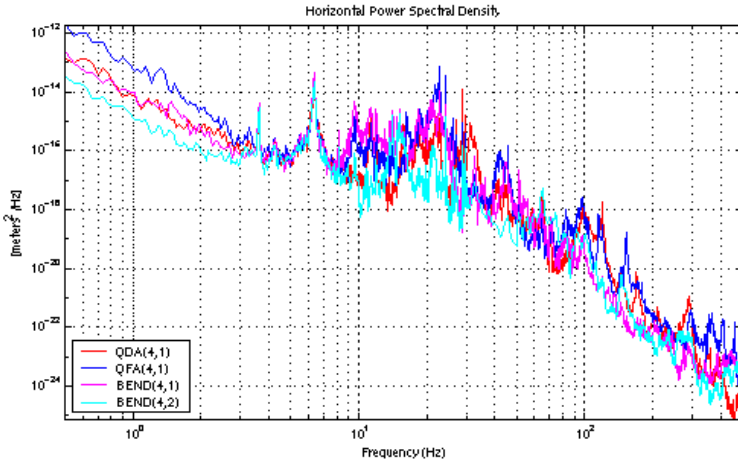
Beam Stability in straight sections w/o Orbit Correction, w/o Orbit Feedback, but w/ Insertion Device Feed-Forward

# ALS Example: Orbit Power Spectral Density



Data taken on 12-12-1999, during a 1.9 GeV user run at 278 mAmps

# Magnet Vibration PSD



# Orbit Correction

By measuring the orbit distortion in  $N$  BPMs along the ring, we find the set of displacements:

$$\mathbf{u}_N = \{u_1, u_2, \dots, u_N\}$$

By using  $M$  correctors magnets, we can find a set of kicks that cancels the displacement of the beam at the BPM positions. This is obtained when:

$$-u_j = \frac{\sqrt{\beta(s_j)}}{2 \sin(\pi\nu)} \sum_{i=1}^M \sqrt{\beta(s_i)} \theta_i \cos \nu \left[ \left| \varphi(s_j) - \varphi(s_i) \right| + \pi \right] \quad j = 1, 2, \dots, N$$

Or in matrix representation, when:

$$-\mathbf{u}_N = \mathbf{M}\boldsymbol{\theta}_M \quad \text{with} \quad M_{ji} = \frac{\sqrt{\beta(s_j)\beta(s_i)}}{2 \sin(\pi\nu)} \cos \nu \left[ \left| \varphi(s_j) - \varphi(s_i) \right| + \pi \right]$$

The kicks that need to be applied to the steering magnets for correcting the closed orbit distortion, can be obtained by inverting the previous equation:

$$\boldsymbol{\theta}_M = -\mathbf{M}^{-1}\mathbf{u}_N$$

The elements of the **response matrix**  $\mathbf{M}$ , can be calculated from the machine model, or measured by individually exciting each of the correctors and measuring the induced displacement in each of the BPMs.



# Orbit Correction Methods

- Simplest method is the **direct inversion** of the orbit response matrix (equal number of BPMs and correctors).
- In case of unequal numbers use **least square** correction (minimizing the sum of the quadratic deviations from the nominal orbit) often with additional constraint to minimize average corrector strength.
- **MICADO/MEC** is a modification of LSQ. It iteratively searches for the single most effective corrector, calculates its correction strength, finds the next most effective corrector, calculates the correction using those two, ...
- **SVD** uses the so called singular value decomposition. In this method small singular values can be neglected in the matrix inversion.
- **Local Bumps** allow to keep the orbit 'perfect' locally (sensitive SR user, interaction point, ...) while relaxing the correction elsewhere.

# Singular Value Decomposition

- Any Matrix  $M$  can be decomposed (SVD)

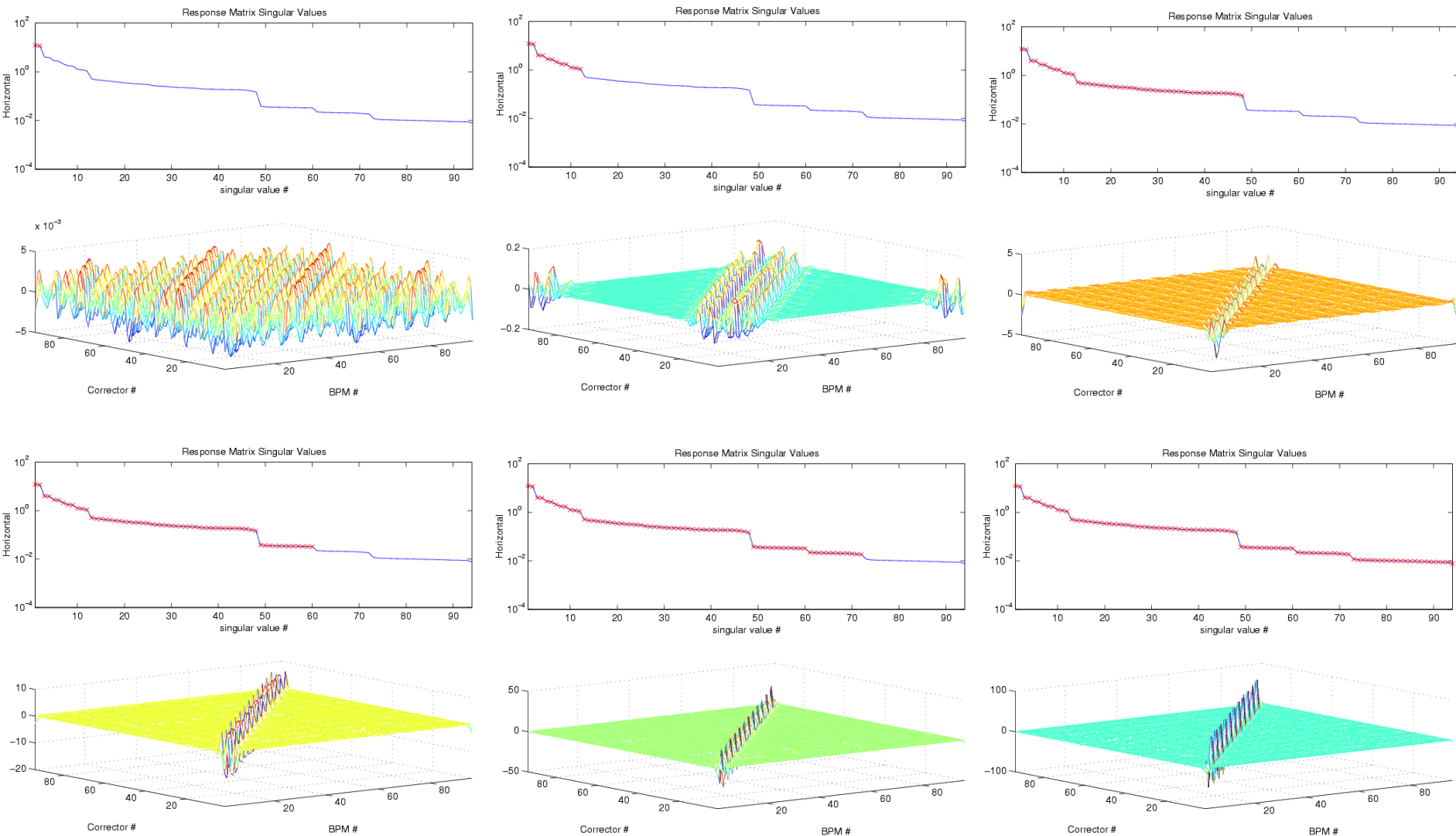
$$M = U \cdot \Sigma \cdot V^T = \sum_i \vec{u}_i \sigma_i \vec{v}_i^T$$

- Where  $U$  and  $V$  are orthogonal matrices (i.e.  $U \cdot U^T = \mathbf{1}$   $V \cdot V^T = \mathbf{1}$ ) and  $\Sigma$  is diagonal and contains the  $(\sigma_i)$  singular values of  $M$ .
- Examples:
  - $M$  is the orbit response matrix
    - $U$  contains an orthonormal set of BPM vectors
    - $V$  contains an orthonormal set of corrector magnet vectors
- Because of orthogonality the inverse of  $M$  can be simply calculated:

$$M^{-1} = V \cdot \Sigma^{-1} \cdot U^T = \sum_i \vec{v}_i \frac{1}{\sigma_i} \vec{u}_i^T.$$

Singularities and small singular values can be removed by removing columns of  $U$  &  $V$ .

## Example: SVD inverted matrix vs. number of SVs



# Trade-offs of Correction Methods

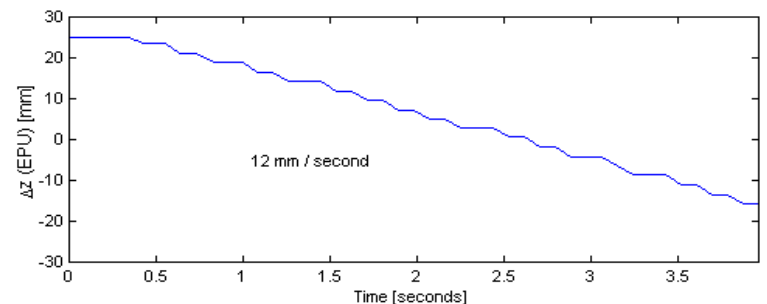
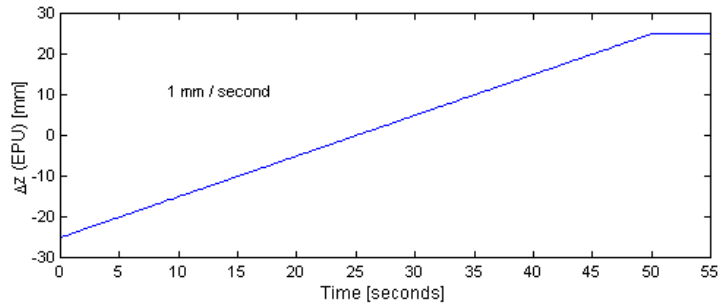
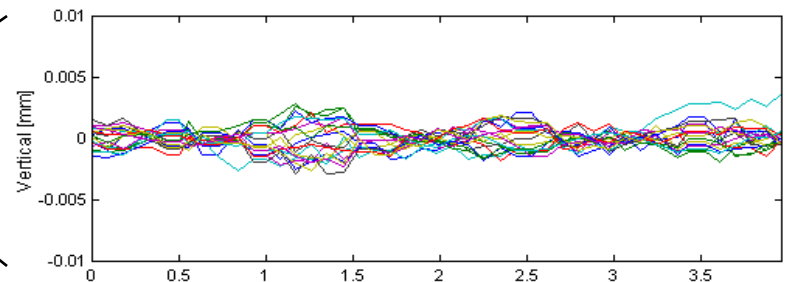
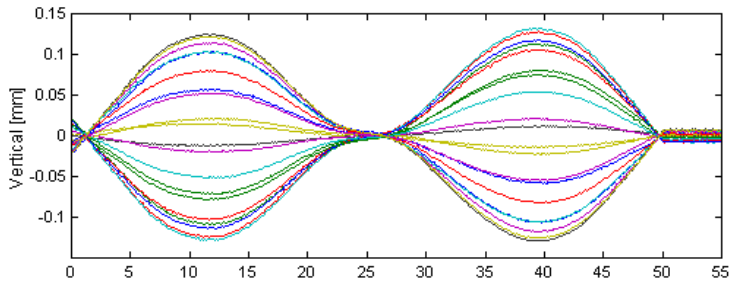
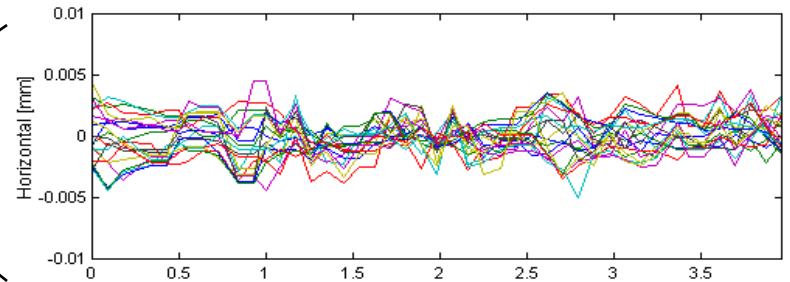
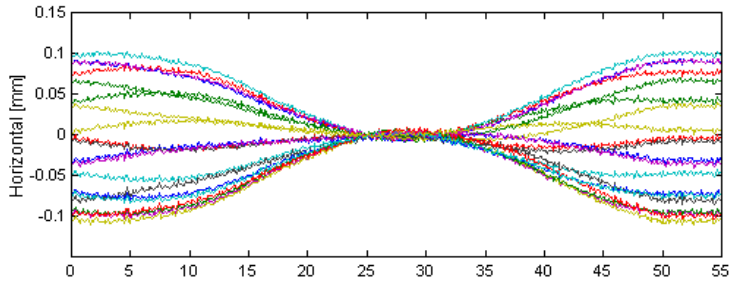
- **Least square or direct matrix inversion**
  - Disadvantages:
    - Have to trust every BPM reading
    - BPM and corrector locations very critical (to avoid unobservable bumps)
  - **Advantages:**
    - Minimizes OBSERVABLE orbit error
    - Works well for distributed/numerous errors
    - localizes the correction.
- **MICADO**
  - works well for few dominant errors (IR quads in colliders)
  - Does not allow good correction for many errors.
- **SVD**
  - allows to adjust behavior based on requirements.
  - **Most light sources nowadays use SVD.**

# Insertion Device Compensation

# EPU Feed Forward Orbit Correction

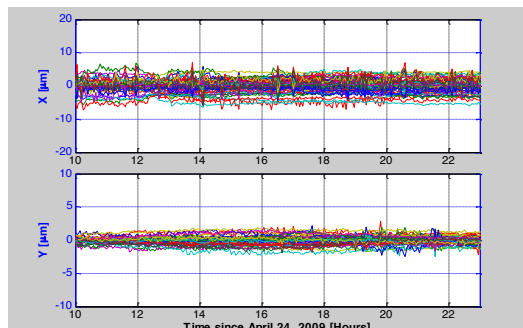
Orbit Error without Feed Forward Correction

200 Hertz Feed Forward Correction

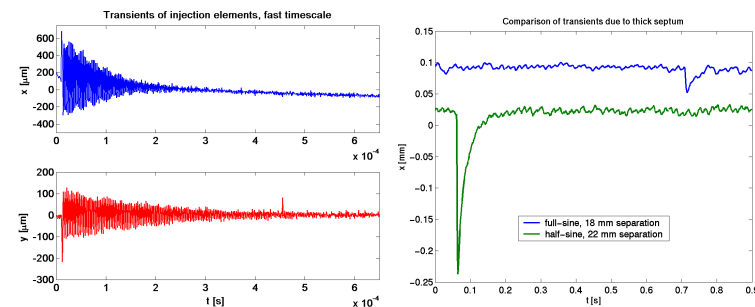
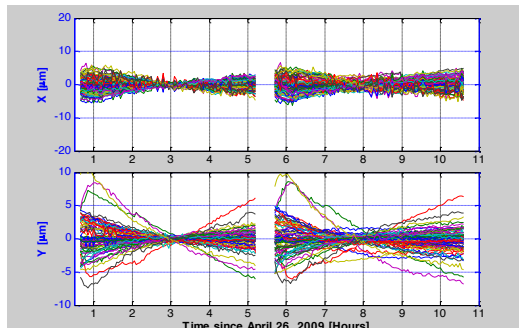


# Orbit Feedback

# Long Term Stability (with Feedback)



ALS: mid term orbit stability (with+w/o Top-off)



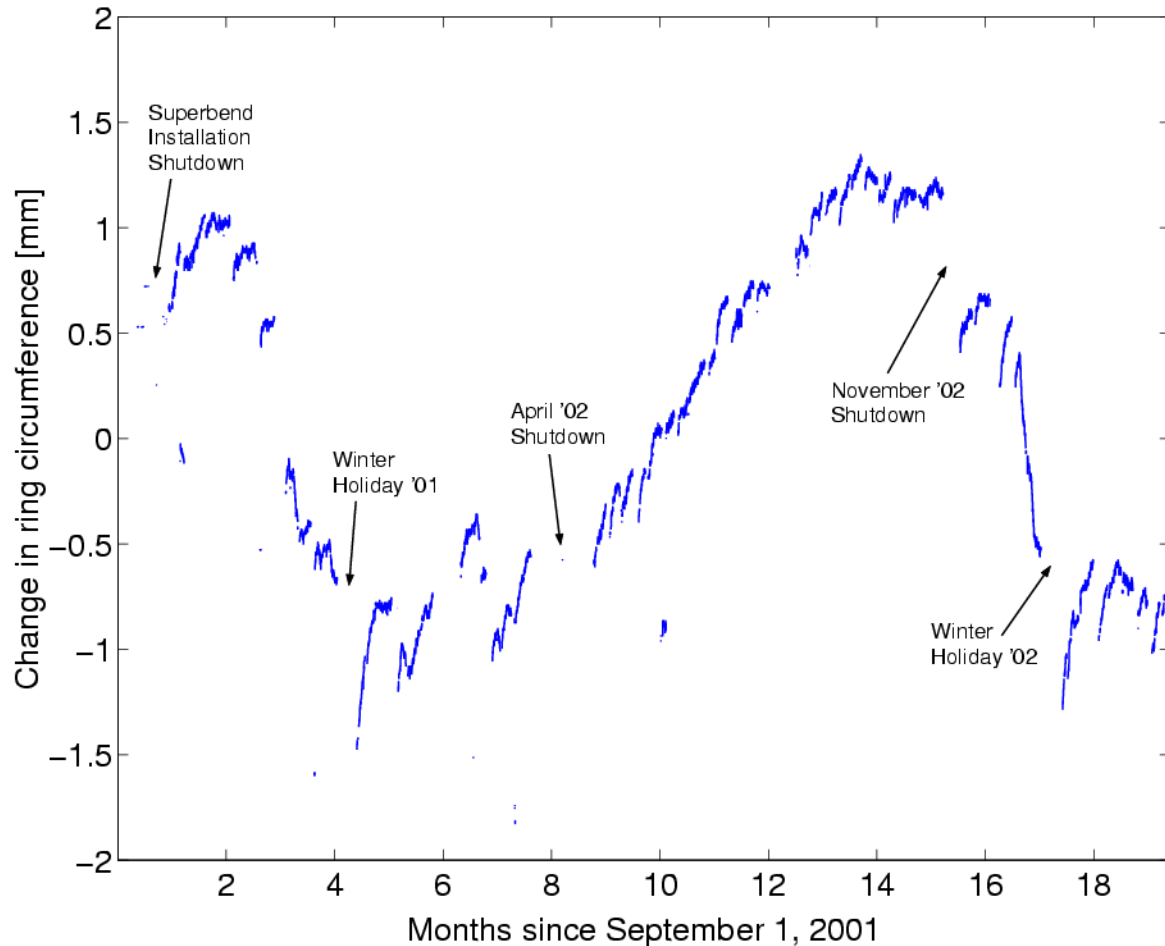
ALS: injection transients (fast+slow)

- **Top-off greatly improves the mid- and long-term stability (also for user beamline optics)**
  - It does present some additional challenges in form of injection transients, however, currently the benefits greatly outweigh those.
  - Injection transients can be improved with better injection element design (magnets and pulsers), use of transverse multibunch feedbacks, or use of multipoles as injection kickers



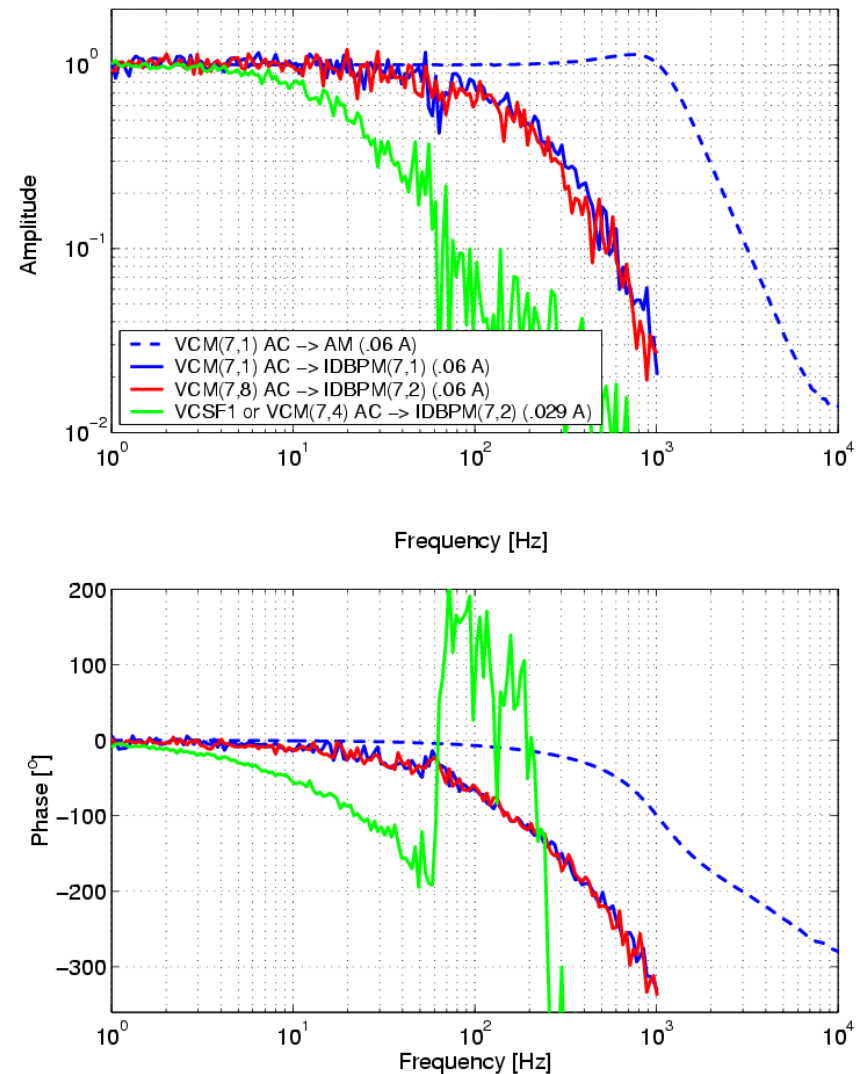
# RF Frequency Feedback

- Circumference of ring changes (temperature inside/outside, tides, water levels, seasons, differential magnet saturation, ...)
- RF keeps frequency fixed – beam energy will change
- Instead measure dispersion trajectory and correct frequency (at ALS once a second)
- Can see characteristic frequencies of all the effects in FFT (8h, 12h, 24h, 1 year)
- Verified energy stability (a few  $10^{-5}$ ) with resonant depolarization

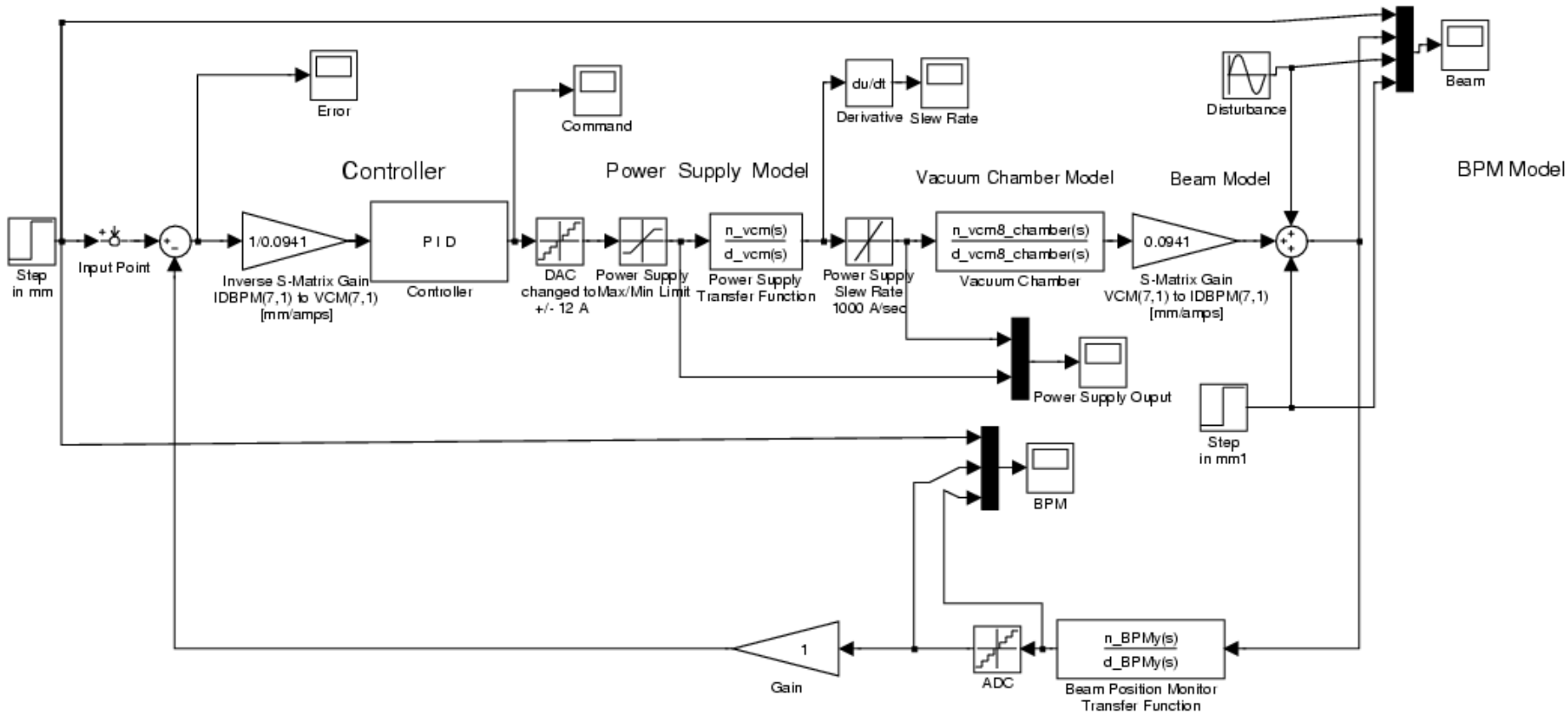


# Fast Orbit Feedback

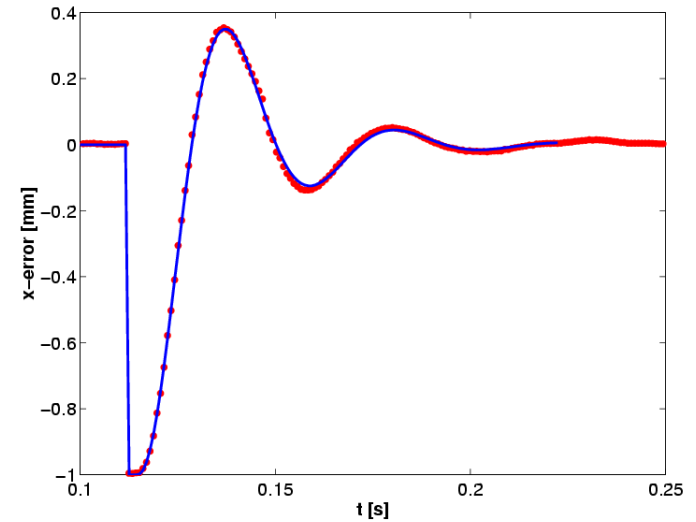
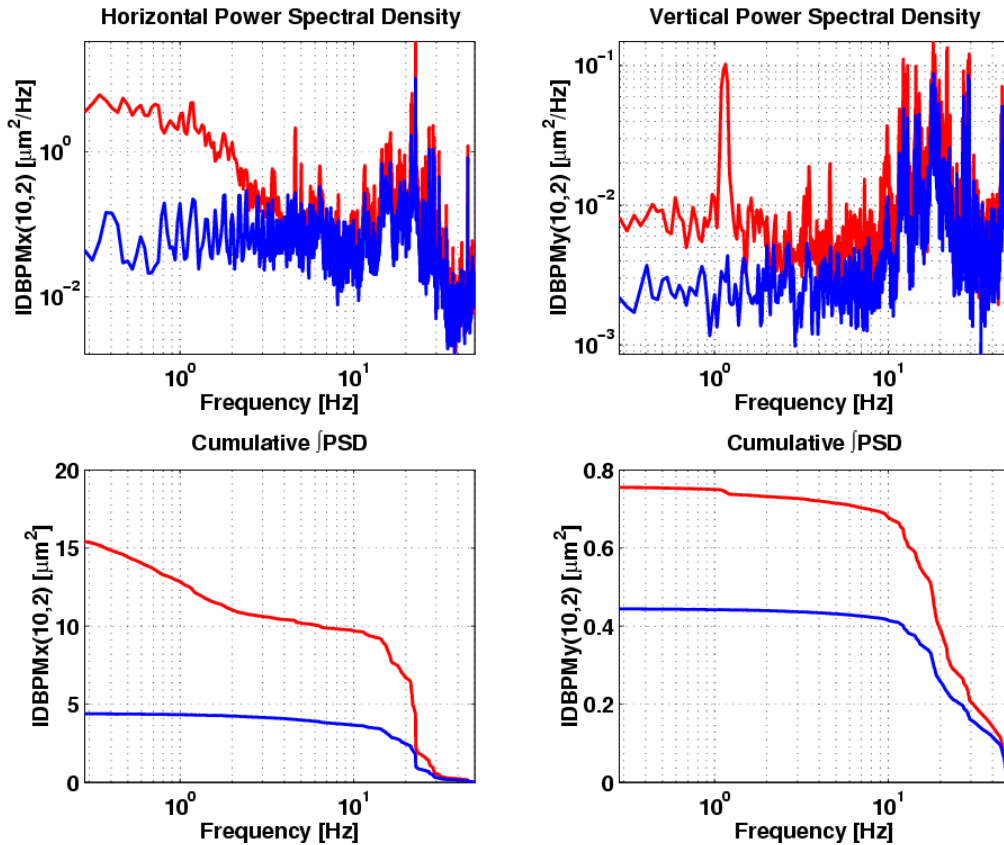
- Time response of all elements becomes important!
- Controller type used is often PID
- System often are distributed (ALS: 12 crates, about 60 BPMs, 22 correctors each plane)



# Simulink model of one channel of system



# ALS Performance of Fast Orbit Feedback at ALS



Comparison of orbit PSDs with and without fast feedback.  
 Fast orbit feedbacks are in use at most light sources: APS, NSLS, ESRF, SLS, ...

Comparison of simulated (Simulink) and measured step response of feedback system in closed loop in a case where PID parameters were intentionally set to create some overshoot.

# Summary (Orbit Stability)

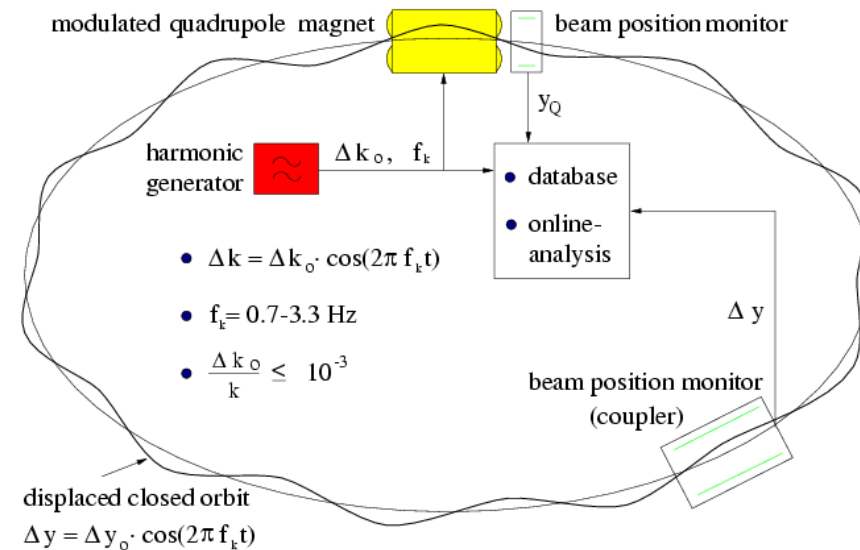
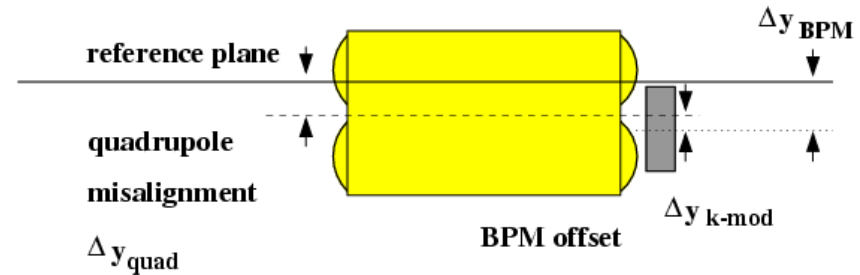
- Stability (orbit, beamsizes) is one of the most important performance criteria at accelerators
- Many different methods for position and size measurement exist, tailored to specific needs. Best resolutions are nm scale.
- Multiple noise sources perturb the beam.
  - Passive noise reduction methods helps.
- Different correction algorithms are available. Advantages depend on the situation.
- Orbit feedbacks are used routinely, nowadays with several kHz update rate.

# Beam Based Alignment

- BPMs centers are not known well enough relative to center of magnetic elements (vacuum chamber positioning, button positions, button attenuations, cable attenuations, signal electronics asymmetries, ...)
- Want to correct orbit to the center of magnetic elements to achieve optimum performance
- Non centered beam can reduce physical/dynamic aperture
  - in quadrupoles: spurious dispersion, larger sensitivity of closed orbit to power supply ripple
  - in sextupoles: gradient errors (horizontal offsets), coupling errors (vertical offsets)
- Allows to link beam position (photon beams) to magnet alignment grid – helps to allow predictive optimum alignment of beamlines

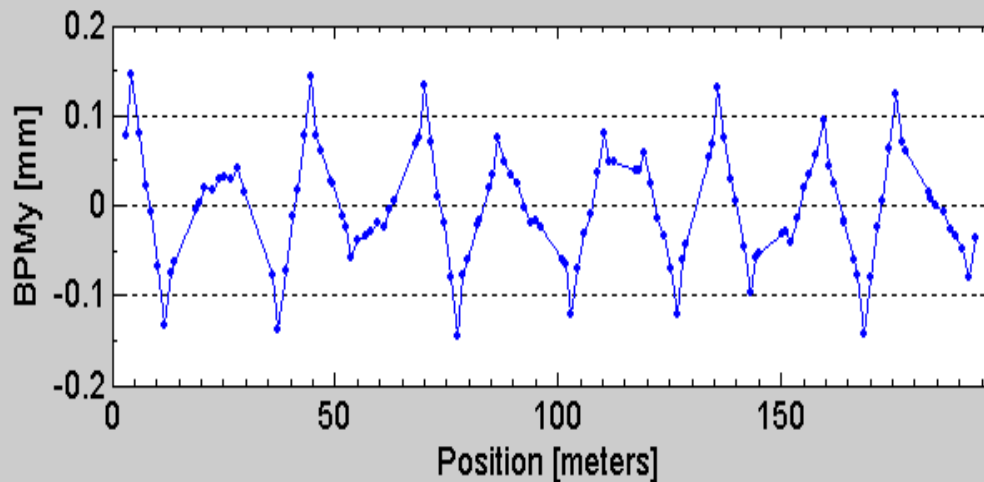
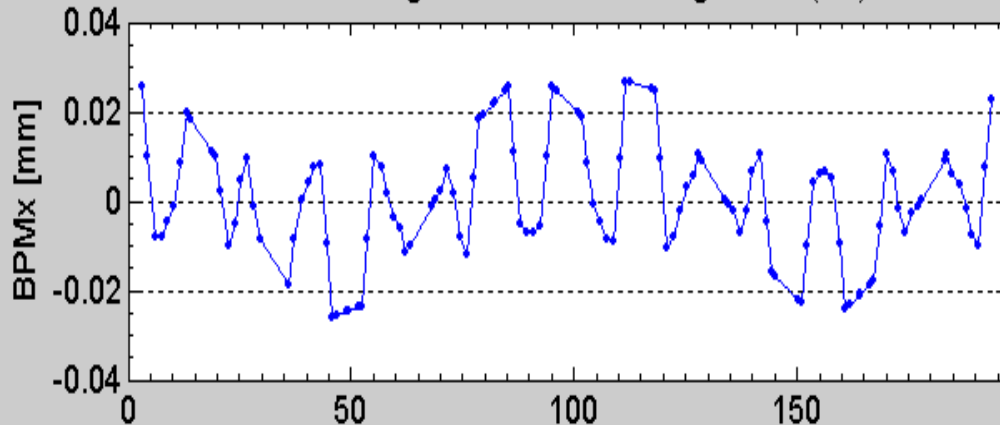
# Beam Based Alignment: Method 1

- BPM centers can be determined relative to adjacent quadrupole (or sextupole, skew quadrupole, using other techniques).
- Basic principle is that a change in quadrupole current will change the closed orbit if the beam does not pass through the quadrupole center.
- Sweeping the beam across a quadrupole and changing the quadrupole strength allows to find the centers.



## BBA, Method 2

Orbit Change Due to a 5% Change in QF(7,1)



Orbit change for a quadrupole change  
(A. Wolski & F. Zimmermann)

$$\Delta x(s) = -x_{off} \frac{C(s, s_0)K_f - C(s, s_0)K_i}{1 - C(s, s_0)K_i}$$

$$C(s, s_0) = \frac{\sqrt{\beta(s)\beta_0}}{2 \sin \pi \nu} \cos(|\psi(s) - \psi_0| - \pi \nu)$$

$x_{off}$  = Initial offset at the quadrupole

$K_i$  = Initial focusing value

$K_f$  = Final focusing value

$\Delta x$  = Transverse position

$\Delta x'$  = Kick strength [radians]

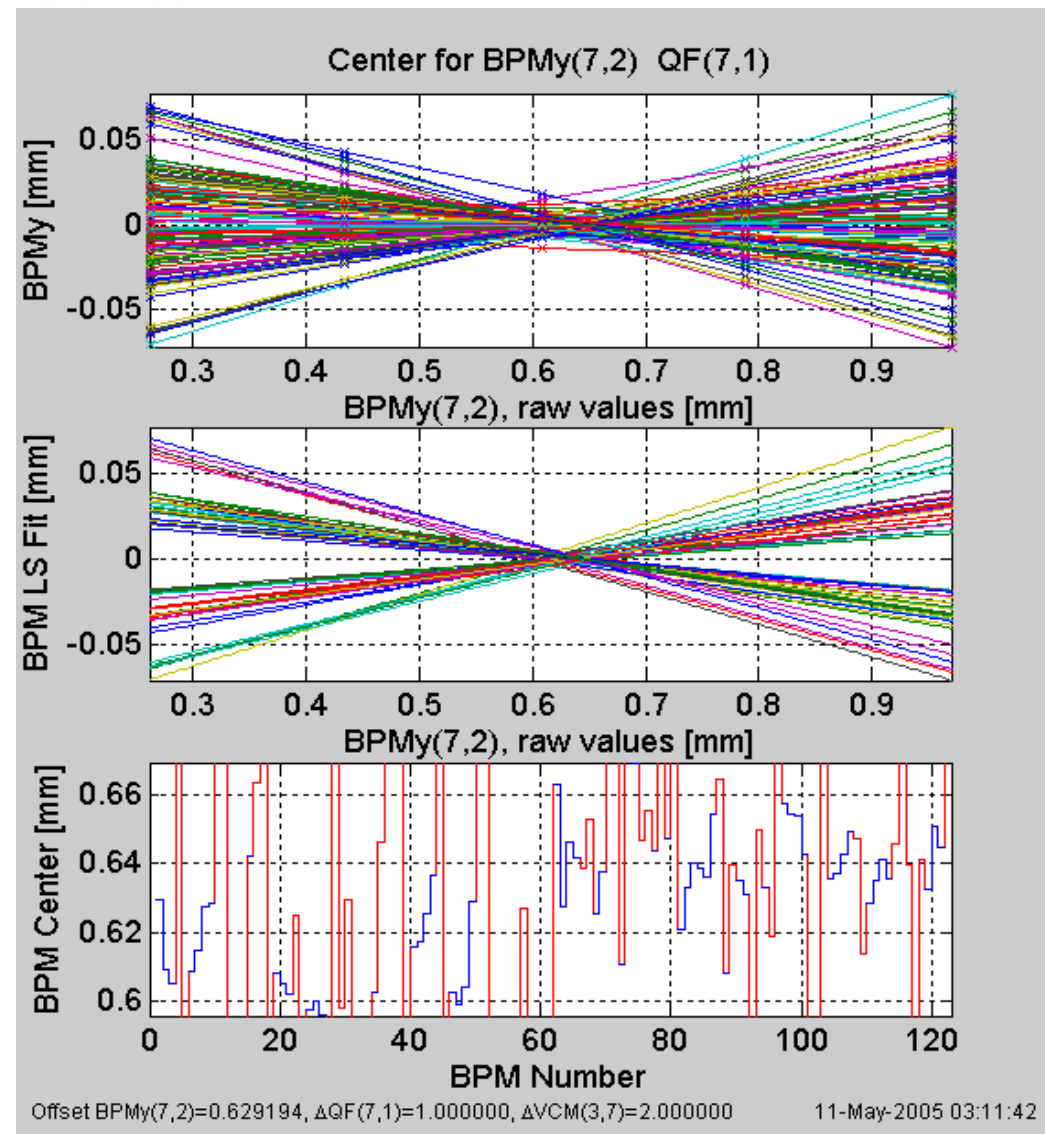
$\beta$  = Beta function

$\psi$  = Phase advance



# Method 3: MML Beam Based Alignment

- The offset of all quadrupoles at ALS (and many other accelerators using the MML) can be found with beam based alignment.
- The algorithm is fully automated.
- BPM offset at ALS are fairly significant (rms of 300-500 microns) but very stable.
- Offsets are typically measured annually or after hardware changes or realignment.
- Main problem were systematic errors due to C-shaped magnets.



# Summary

- Orbit Stability is one of the most important performance criteria at accelerators
- Many different methods for position measurement exist, tailored to specific needs. Best resolutions are nm scale.
- Multiple noise sources perturb the orbit. Passive noise reduction methods can improve the situation a lot.
- Different correction algorithms are available. Advantages depend on the situation.
- Orbit feedbacks are used routinely, nowadays with several kHz update rate.
- Beam based alignment is essential to guarantee optimum performance of accelerators.

# Further Reading (incomplete list):

- B. Hettel, Rev. Sci. Instr. 73, 3, 1396
- W.H. Press et al., Numerical Recipes, Cambridge U. Press (1988) p. 52
- Presentations at 2<sup>nd</sup> International Workshop on Beam Orbit Stabilization (2002):  
<http://www.spring8.or.jp/ENGLISH/conference/iwbs2002/abstract.htm>
- Presentations at the 3<sup>rd</sup> International Workshop on beam Orbit Stabilization (2004):  
<http://iwbs2004.web.psi.ch/program/orals.html>
- A. Friedman, E. Bozoki, NIM A344 (1994) 269
- J. Carwardine, F. Lenkszus, Proceedings of the 1998 Beam Instrumentation Workshop, <http://www.slac.stanford.edu/pubs/confproc/biw98/carwardine.pdf>

# Backup Slides

# Stripline BPMs

- Stripline structures are also widely used as the “kicker” in transverse and longitudinal feedback systems.

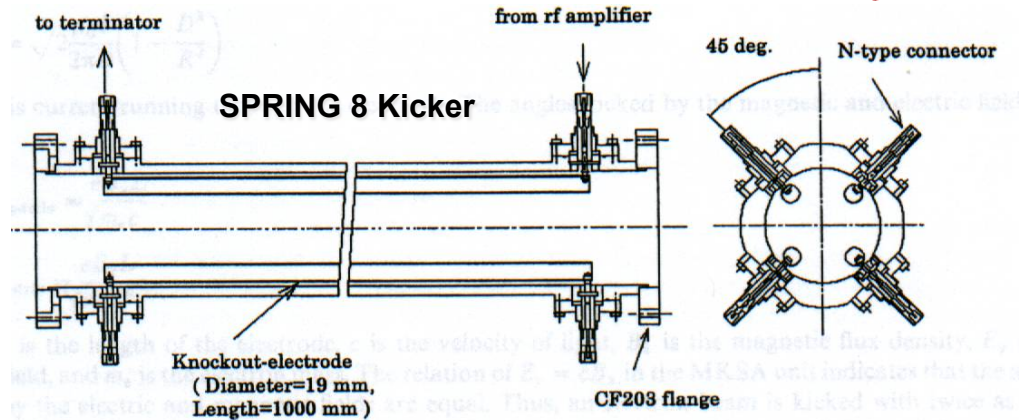
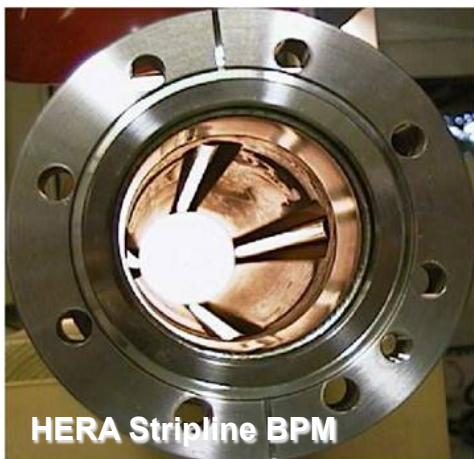
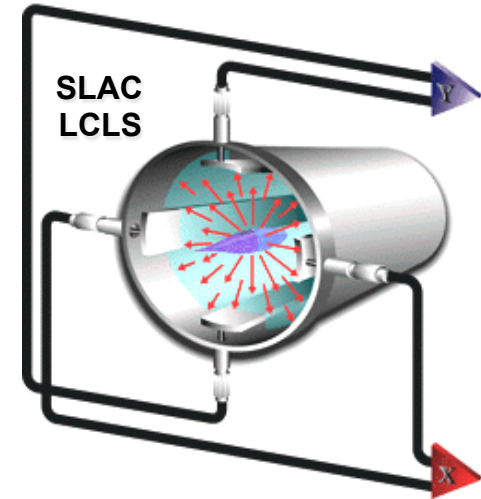
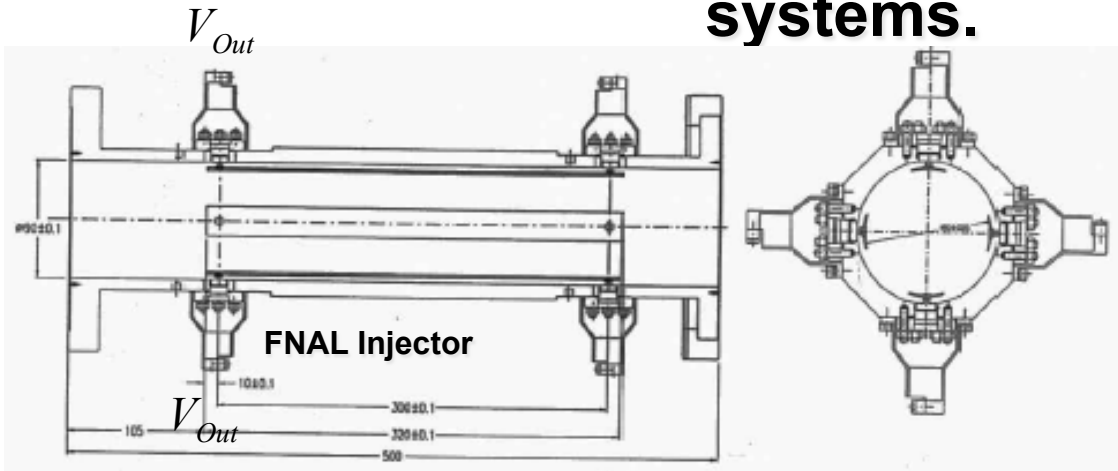
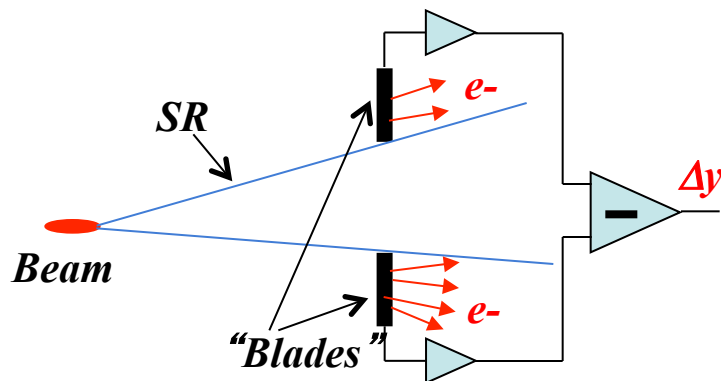
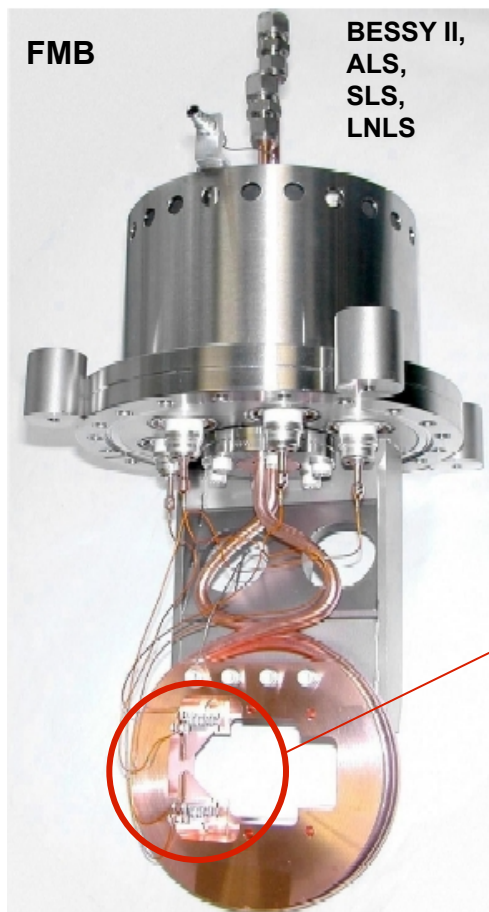


Fig. 6. Cross-sectional view of RFKO electrodes.

# Other BPMs (using Photons)

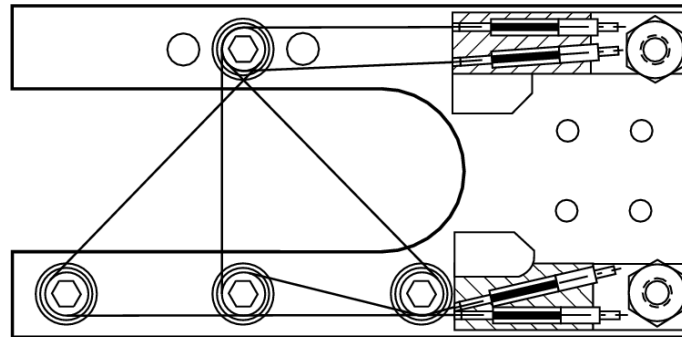
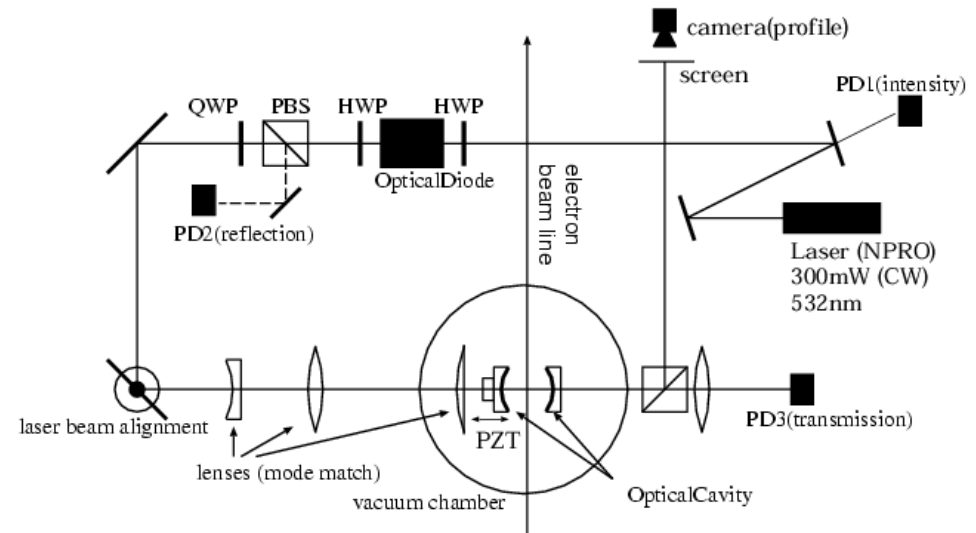
- Synchrotron radiation is abundant in many accelerators – very useful for low noise, non destructive position measurement



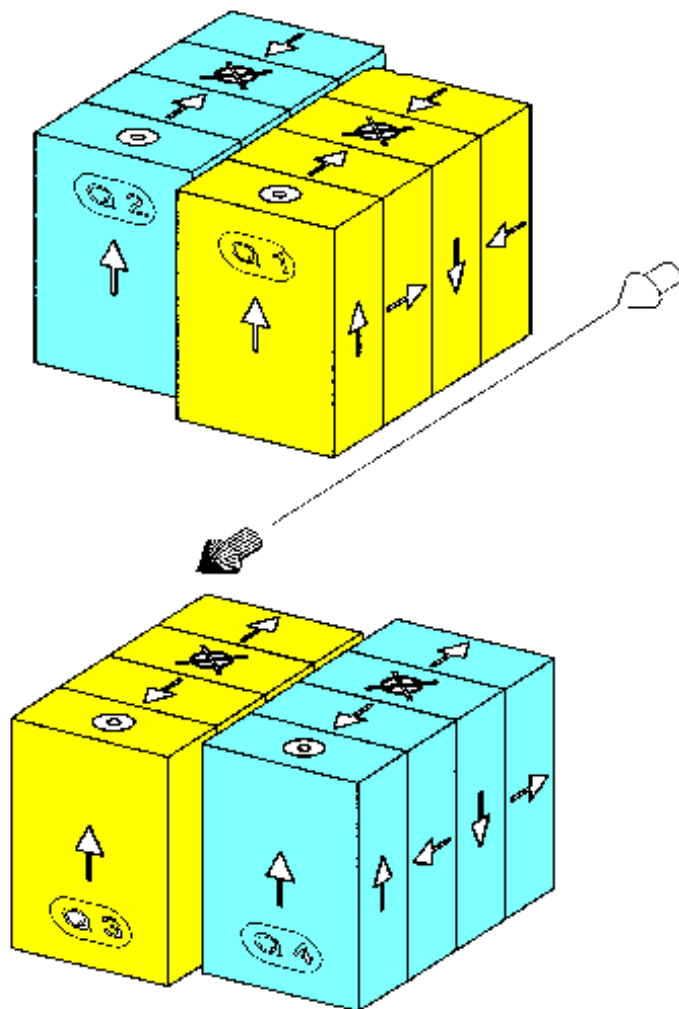
- ❖ Work very well for dipoles in the vertical plane – not so simple for insertion devices
- ❖ Fundamentally limited in the horizontal plane for dipoles

# (Flying) Wire Scanners/Laser Wires/Screens

- Wire Scanners (SLAC/SLC) and screens are mostly used in beamlines and Linacs. Can achieve reasonable high resolution but are usually destructive. Both can measure position and profile.
- Flying wires are less destructive and laser wires (KEK/ATF) are minimally destructive and provide excellent resolution (however they are slow)
- Some laser or interferometer based schemes achieve nm type resolutions.



# Elliptically Polarizing Undulator (EPU)



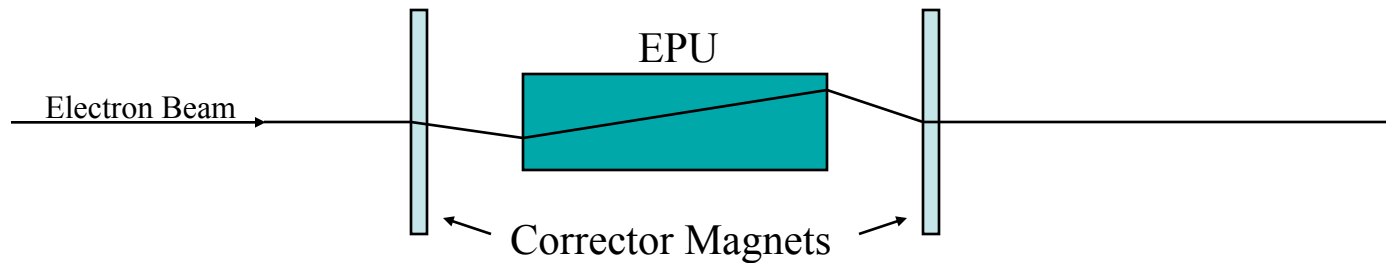
The EPU is different than other insertion devices

- ❖ The jaws can move in two directions (vertically and longitudinally)
- ❖ The motion in the longitudinal direction is fast  
(At the ALS, up to 17 mm/second)

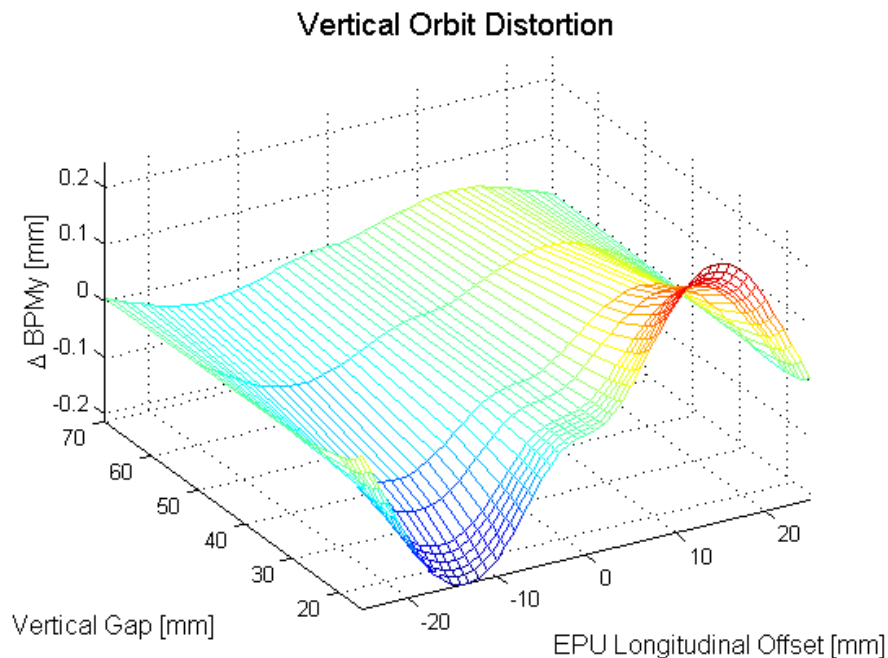
*This makes orbit compensation more difficult than other insertion devices*



# Feed-forward example: EPU



**Mechanically, an ALS EPU can move from left to right circular polarization mode in  $\sim 1$  sec.**



Without compensation the EPU would distort the electron beam orbit by  $\pm 200 \mu\text{m}$  vertically and  $\pm 100 \mu\text{m}$  horizontally. Using corrector magnets on either side of the EPU, 2-dimensional feed forward correction tables are used to reduce the orbit distortion to the  $2\text{-}3 \mu\text{m}$  level. Update rate of feed-forward is 200 Hz.

Feed-forward tables based on beam based measurements are much more accurate than ones based on magnetic bench measurements.

For even faster switching devices (CPW, ...) eddy current effects make beam based optimization even more important.